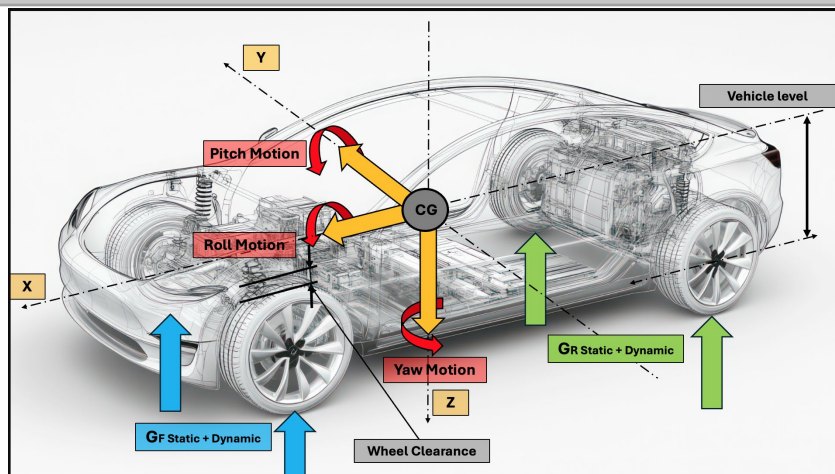


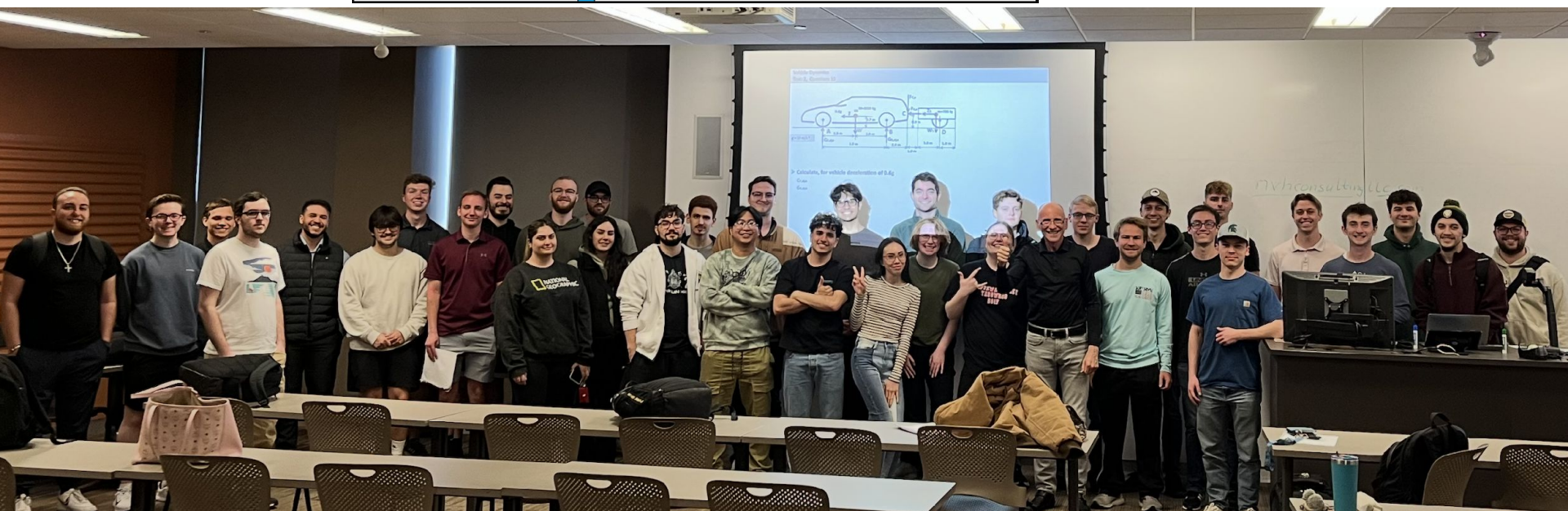


ME 4220 Automotive Engineering Vehicle Dynamics

Johann Pankau



Winter Semester 2025
Vehicle Dynamic
ME 4220 Course



Introduction

Applied mechanics and mathematics utilized in vehicle modeling
Vehicle axis systems, centre of gravity, loads, inertias

Vehicle Dynamics

Longitudinal Dynamics

Dynamic axle loads at acceleration or deceleration
Traction limited acceleration, climbing, traction control
Traction limited braking, brake stability
Brake forces distribution
Vehicle resistances and engine output requirements

Vertical Dynamics

Vibration, noise classification, propagation and phenomenon's
Simple vertical dynamics modeling
Road excitation
Suspension springing and shock absorbing

Lateral Dynamics

Lateral acceleration, forces and slip angle
Low speed cornering
Vehicle under-steering, over-steering and self steering
Vehicle stationary and non-stationary cornering, line change
Lateral dynamics modeling

Interaction between longitudinal, vertical and lateral vehicle dynamics

3-Dimensional interaction
Vehicle pitch and roll motions and General considerations
Vertical Force Variations
Braking, accelerating while cornering, braking on split μ surface
Vehicle Dynamics Target Conflicts

Chassis systems in vehicle dynamics

Suspension design, classification, kinematics and elastokinematics

Introduction to brake systems, and importance in vehicle dynamics control

Tire as major and most important component in vehicle dynamics

History

Requirements

Design / construction

Force transfer and road contact

Longitudinal dynamics: traction and braking

Vertical dynamics: ride and NVH

Lateral dynamics: cornering

Longitudinal dynamics influence on lateral forces: accelerating, braking while cornering

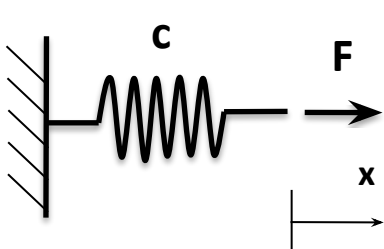
Nonuniformity and vehicle interaction

Tire performances, performances balance and conflicts

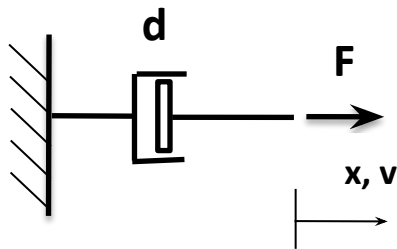
Modeling

1. Introduction

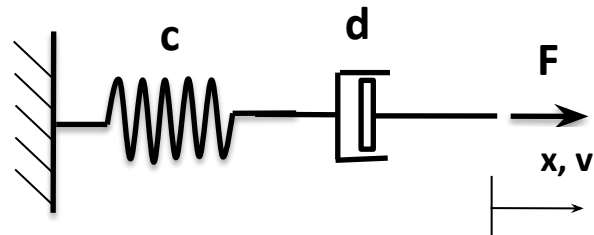
1.1. Applied mechanics and mathematics utilized in vehicle modeling



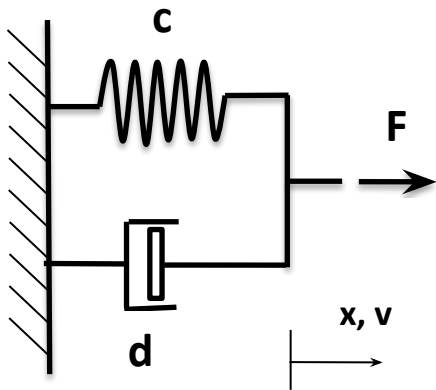
$$F = cx$$



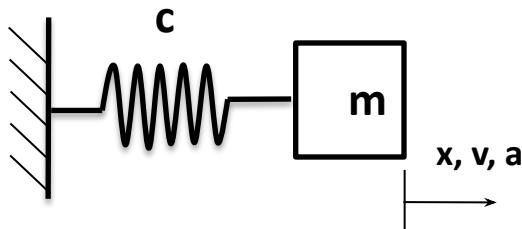
$$F = dv$$



$$v = \frac{dF}{dt} \frac{1}{c} + \frac{F}{d}$$

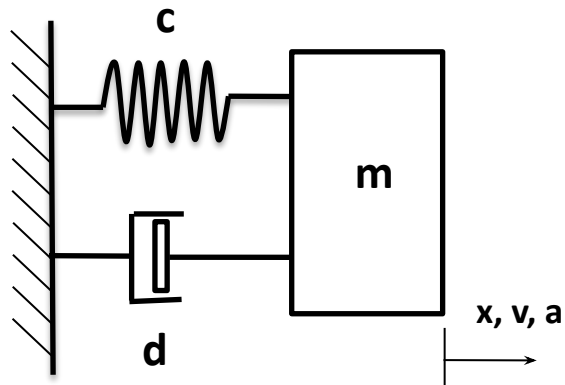


$$F = cx + dv$$



$$cx + ma = 0$$

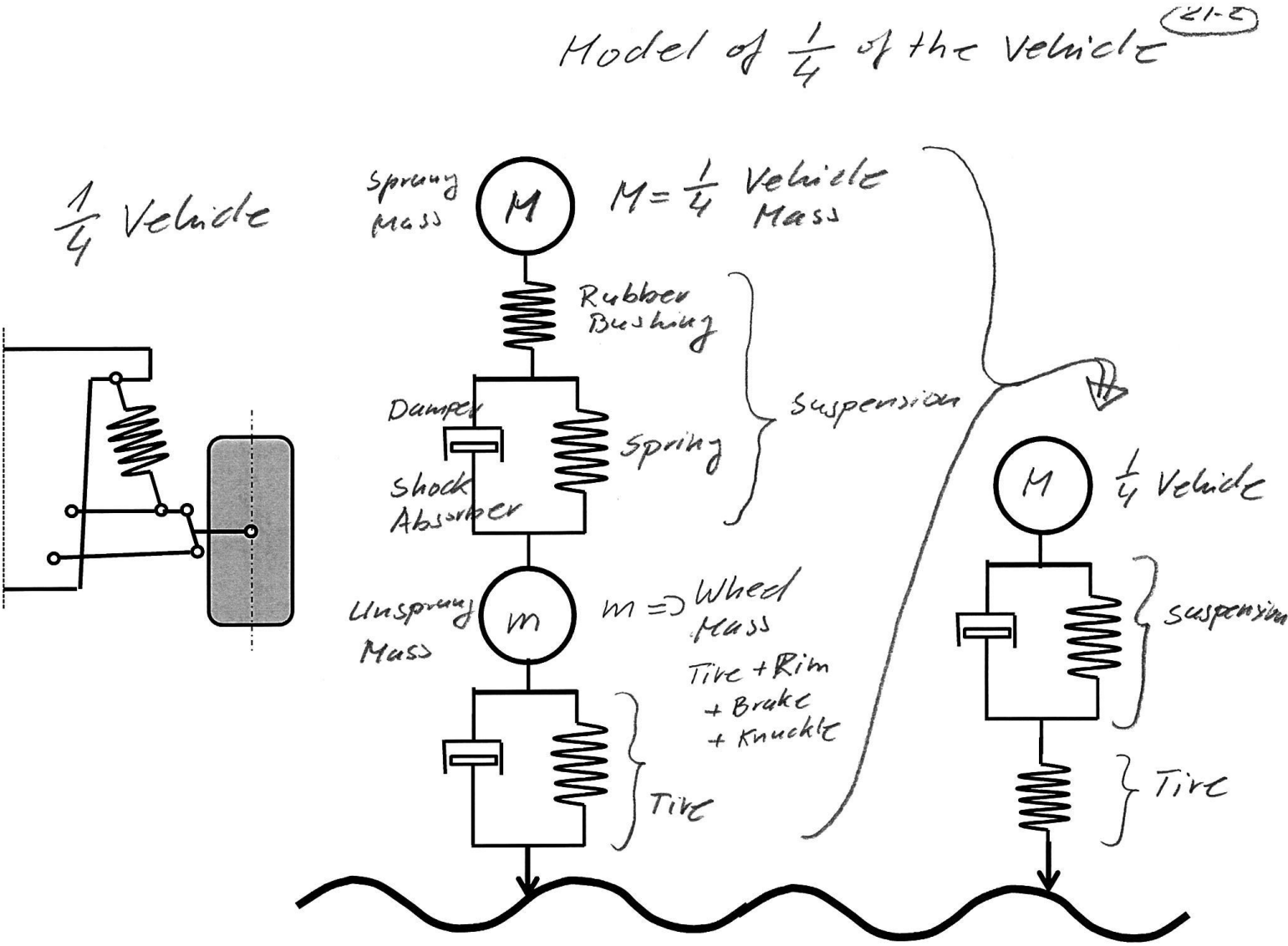
$$\omega = \sqrt{c/m}$$

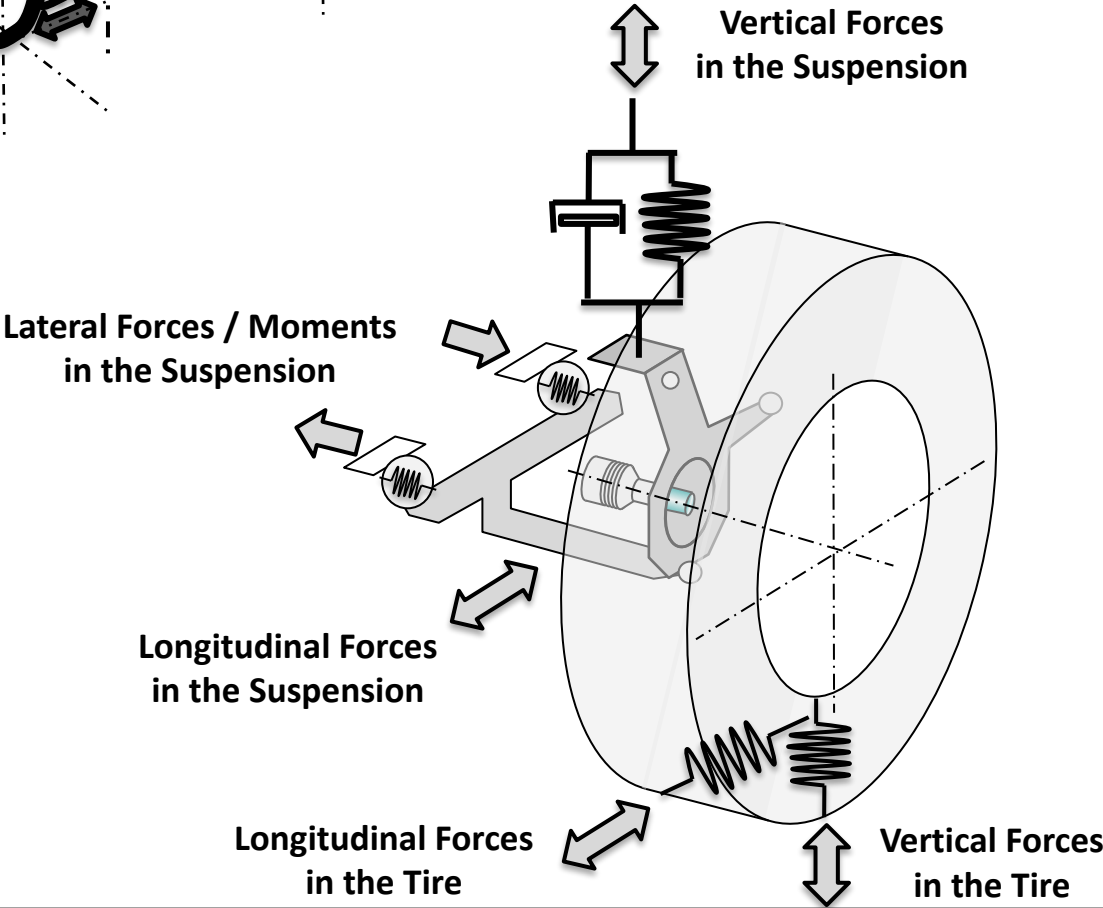
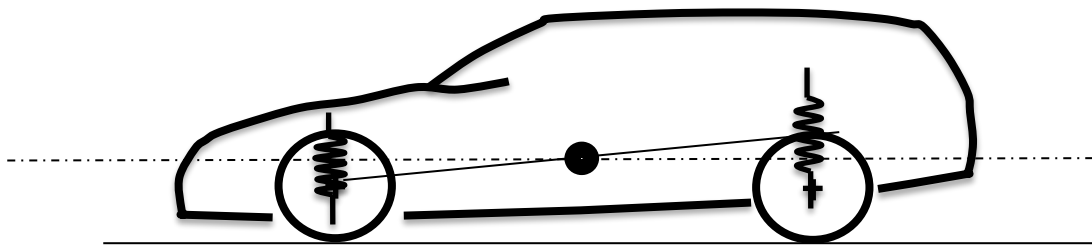
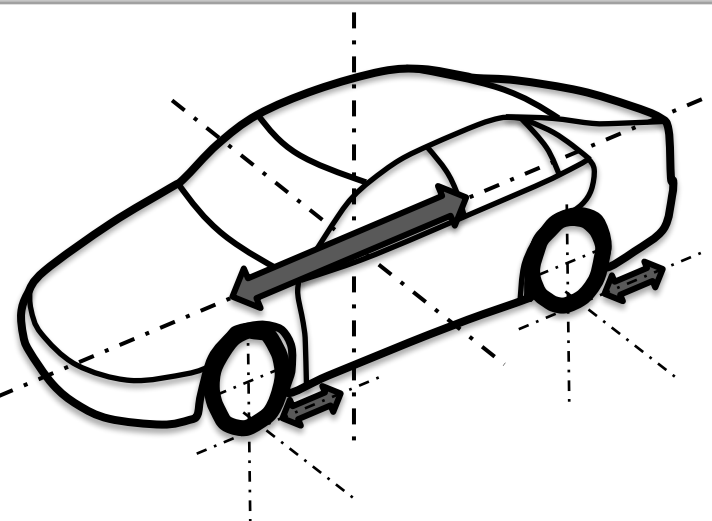


$$cx + dv + ma = 0$$

1. Introduction

1.1. Applied mechanics and mathematics utilized in vehicle modeling



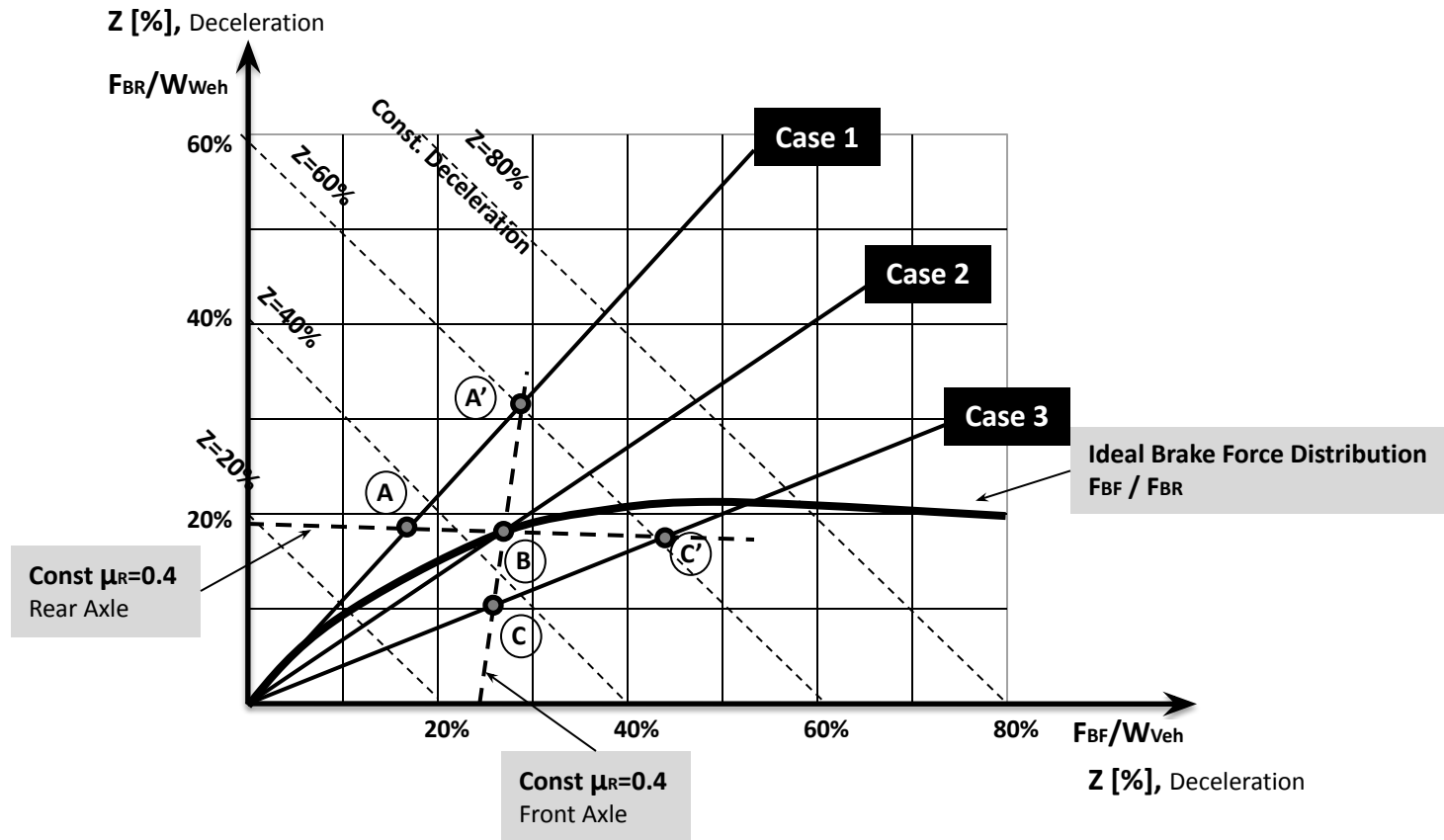


Excitation Forces:

- Acceleration
- Braking
- Load change

2. Longitudinal Dynamics

2.3. Traction limited braking, braking stability



Case 1: Rear wheels blocked first: Unstable Situation

Case 2: Front and Rear wheels blocked at the same time: Unstable Situation, No Steering

Case 3: Front wheels blocked first: Stable Situation, No Steering

Vehicle Output / Power Requirements

During driving following Vehicle Resistances needs to be overcome:

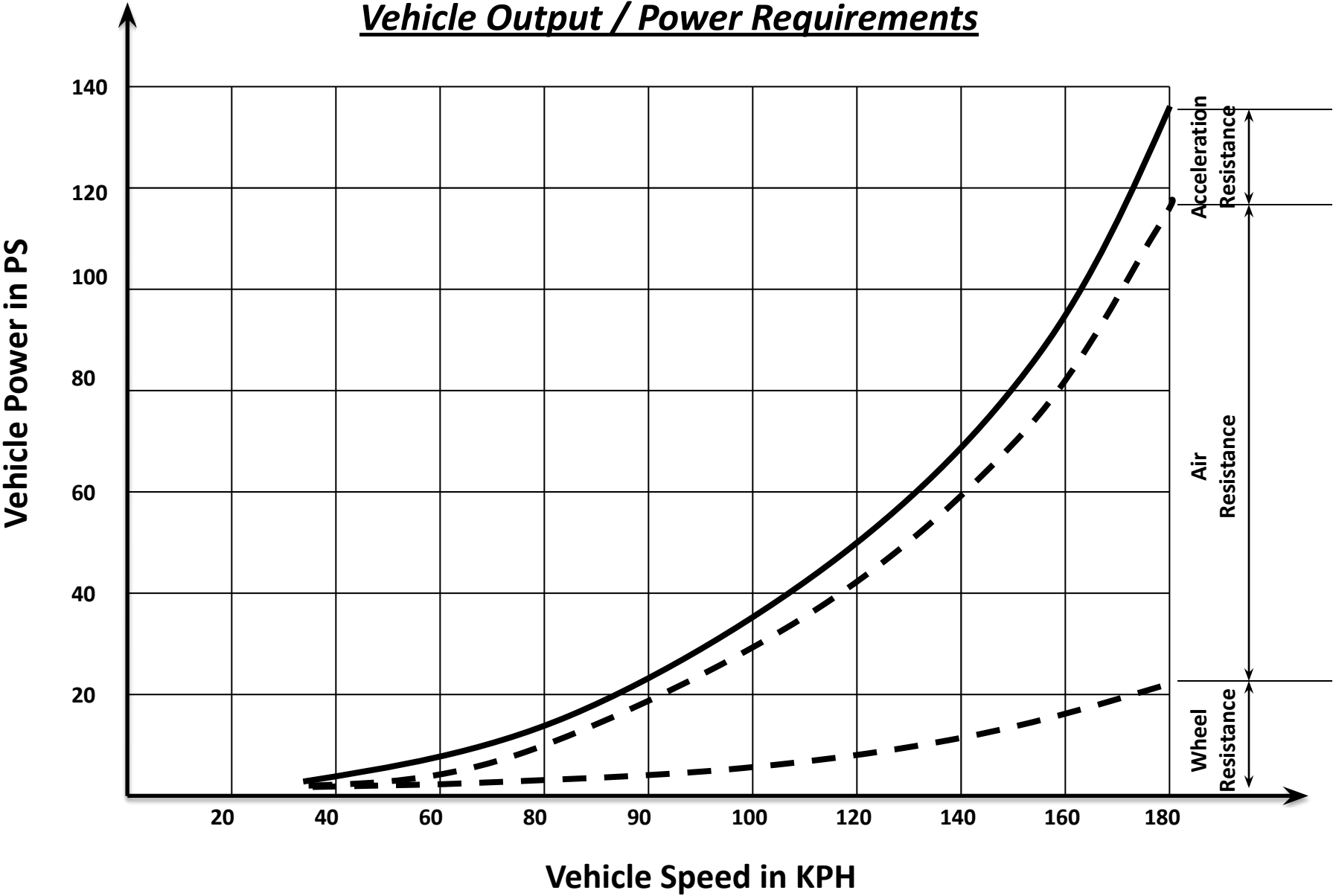
- Acceleration Resistance $F_{R,Acc}$
- Wheel Resistance $F_{R,W}$
- Air Resistance $F_{R,A}$
- Climb Gradient Resistance $F_{R,Climb}$
- Towing Resistance $F_{R,T}$

□ Total Vehicle Resistance: $F_R = F_{R,W} + F_{R,A} + F_{R,Climb} + F_{R,Acc} + F_{R,T}$

Special Cases:

□ constant drive w/o gradient:	$F_R = F_{R,W} + F_{R,A} + F_{R,T}$	$F_{R,Climb} = F_{R,Acc} = 0$
□ constant drive on gradient:	$F_R = F_{R,W} + F_{R,A} + F_{R,Climb} + F_{R,T}$	$F_{R,Acc} = 0$

Vehicle Output / Power Requirements



Vehicle Output / Power Requirements

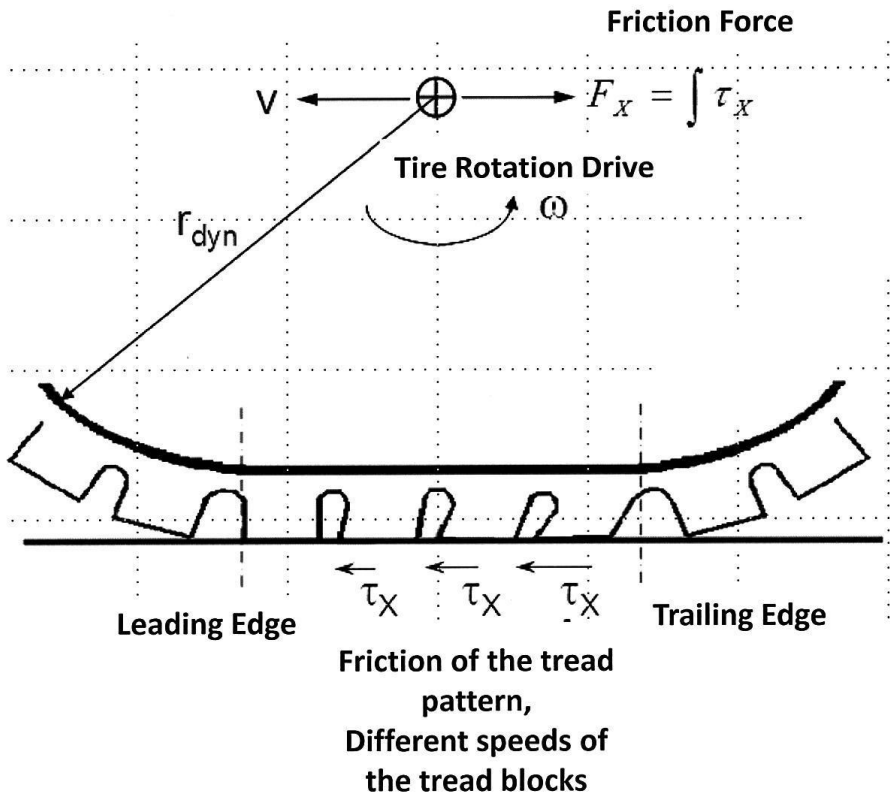
During driving following Vehicle Output / Power is required in order to overcome Vehicle Resistances:

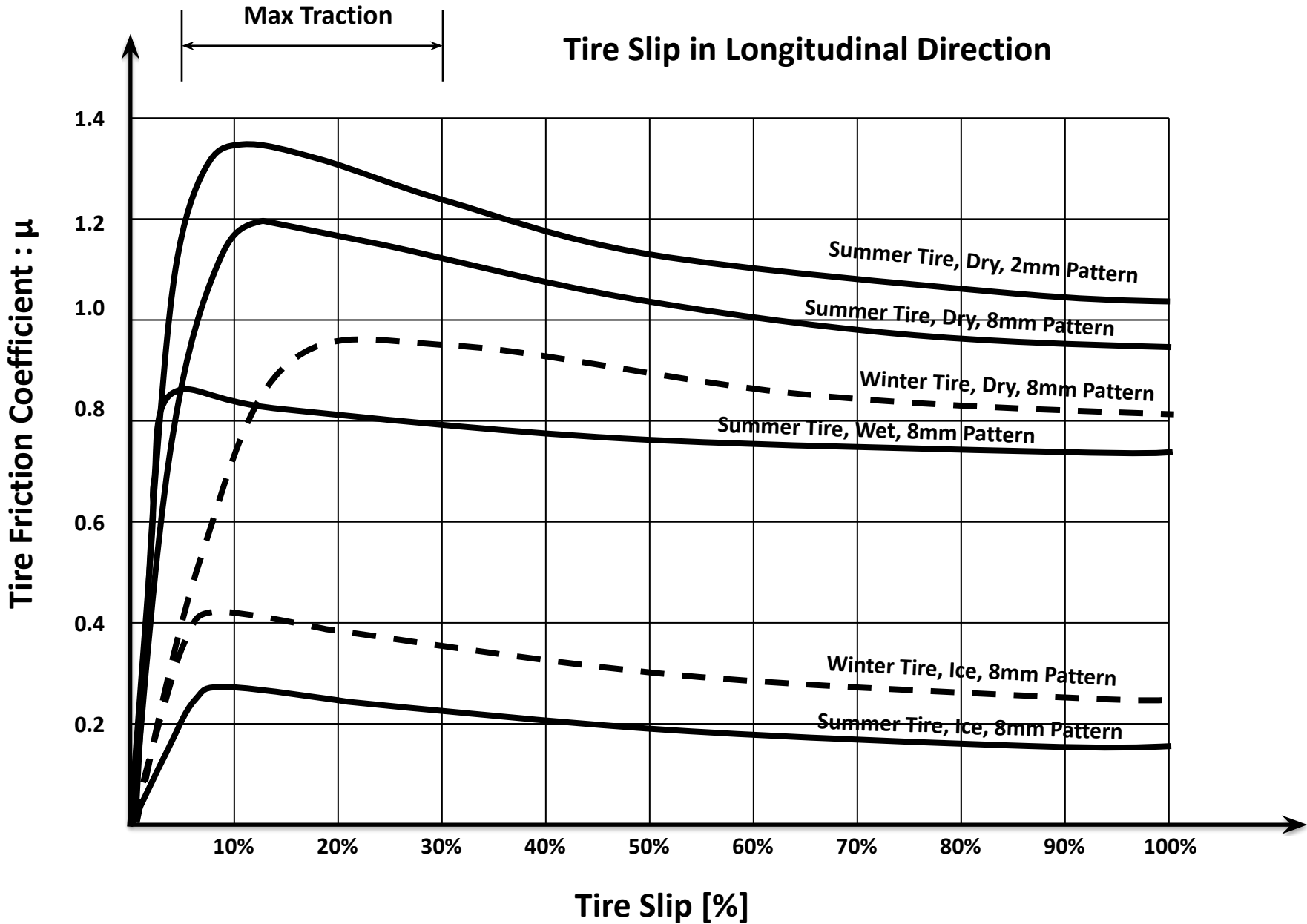
□ **Total Vehicle Resistance Power:**

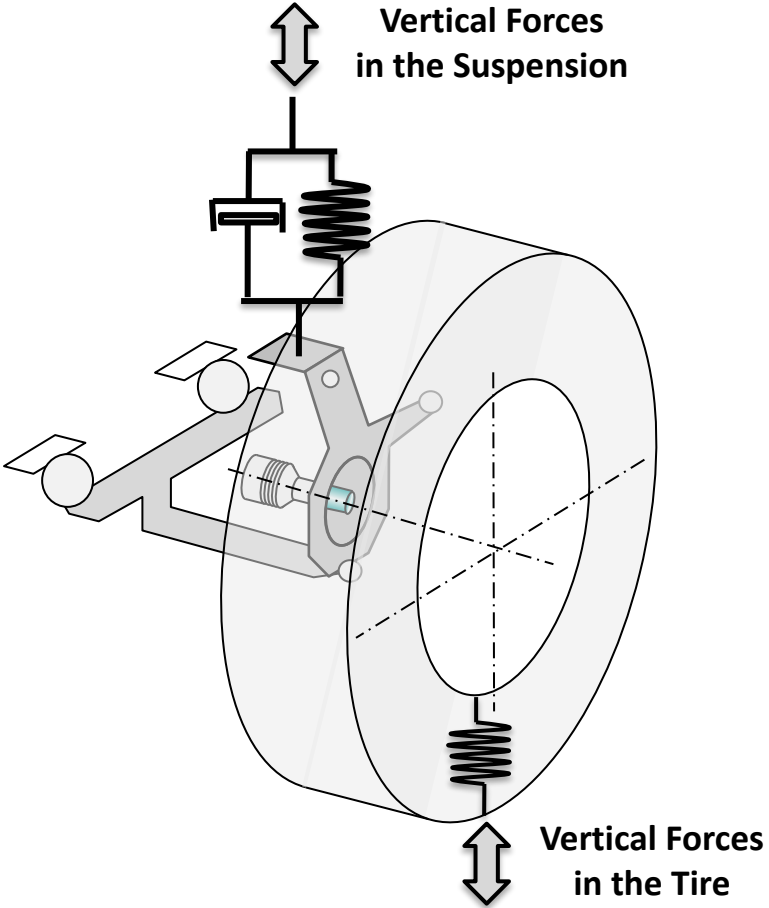
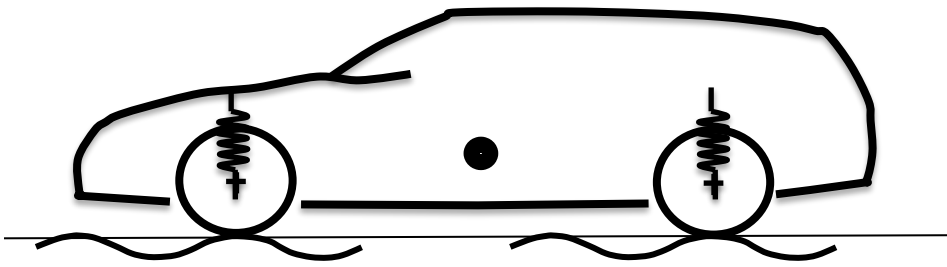
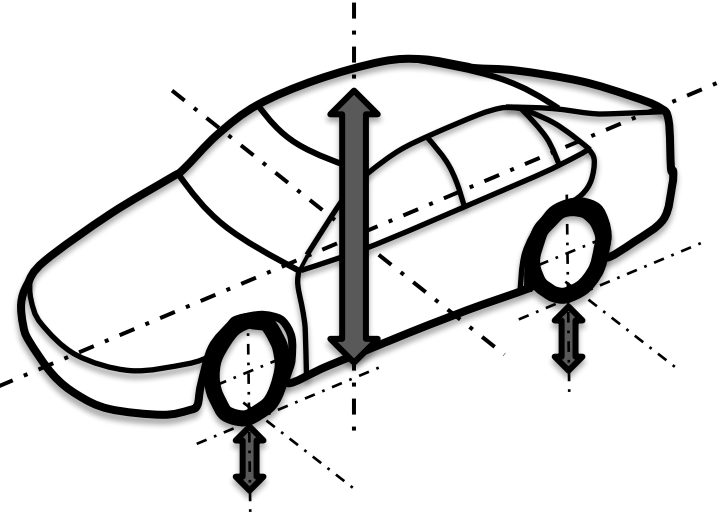
$$P_R = P_{R,W} + P_{R,A} + P_{R,Climb} + P_{R,Acc} + P_{R,T}$$

$$P_R = F_{R,W} v$$

Tire / Wheel Slip *in Longitudinal Direction*







Excitation Forces:

- Dynamic interaction with the Road Surface

3. Vertical Dynamics

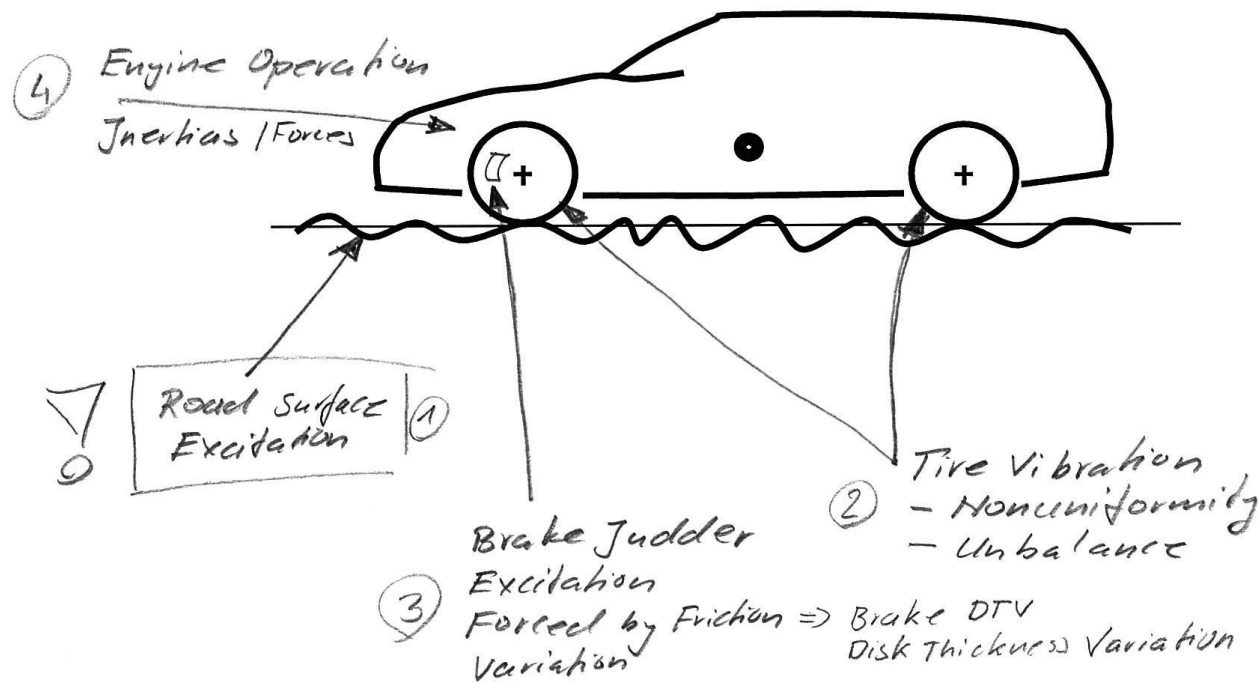
3.1. Vibration, noise classification, propagation and phenomenon's

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136-1

Sources of Vehicle Vertical Vibration

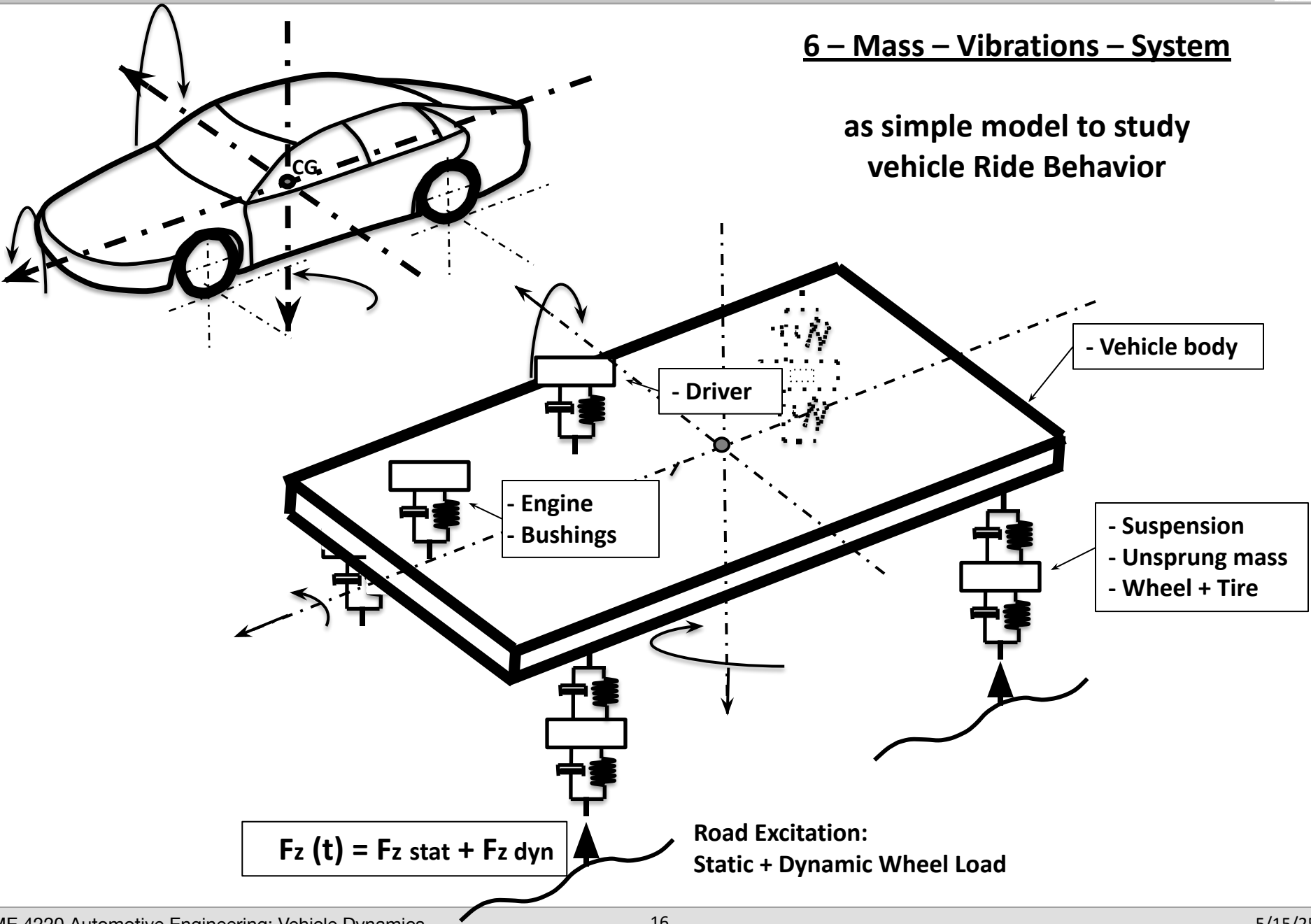
Forced Vibration

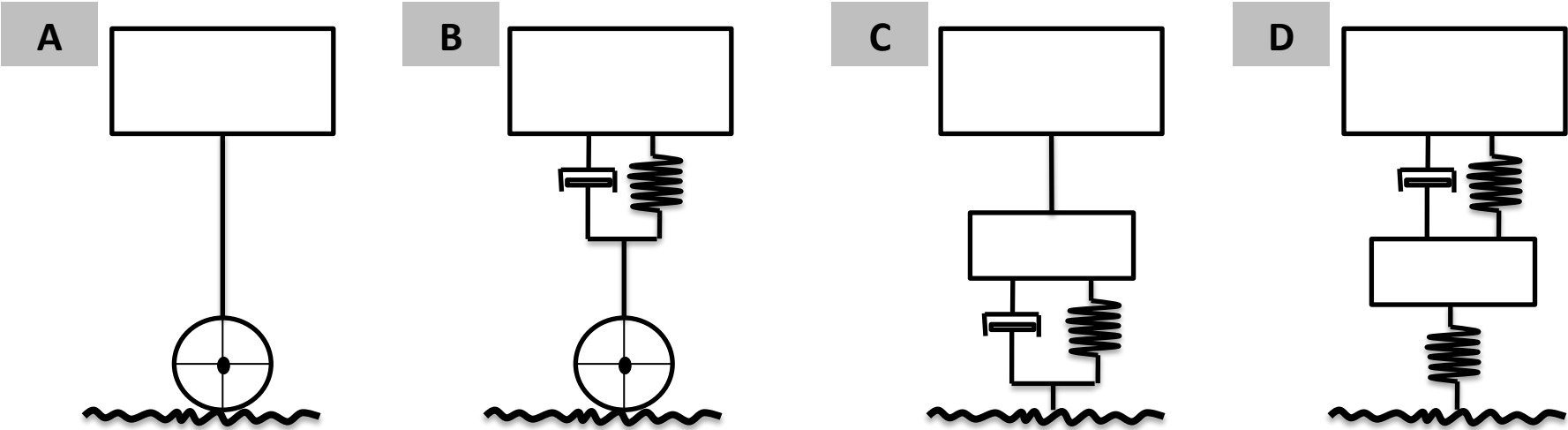
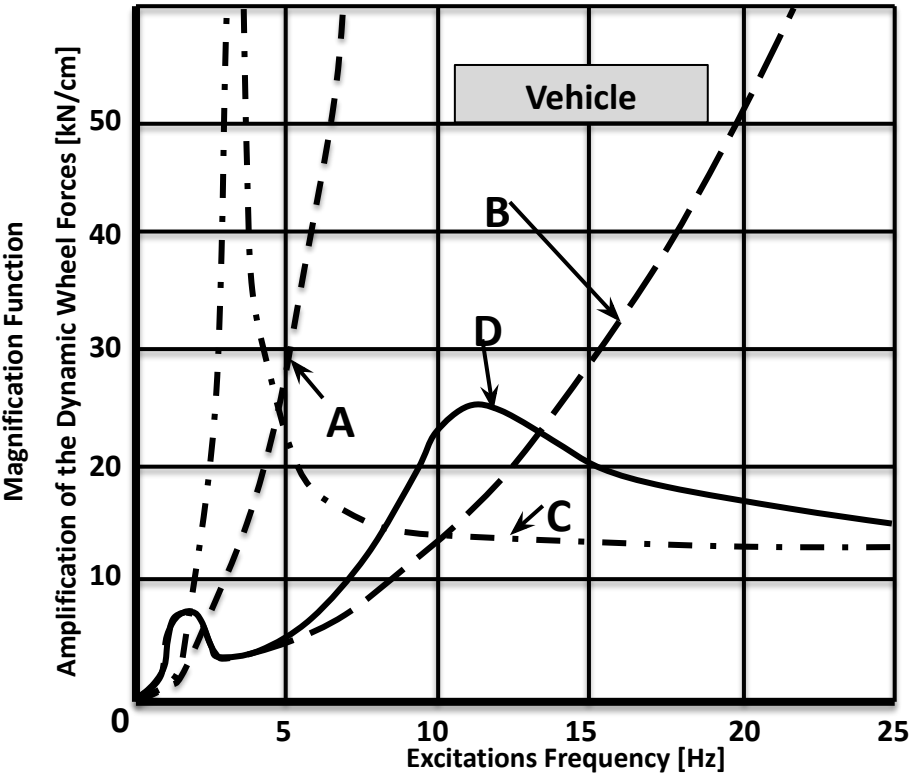
⑤ Driving maneuvers



3. Vertical Dynamics

3.2. Simple vertical dynamics modeling

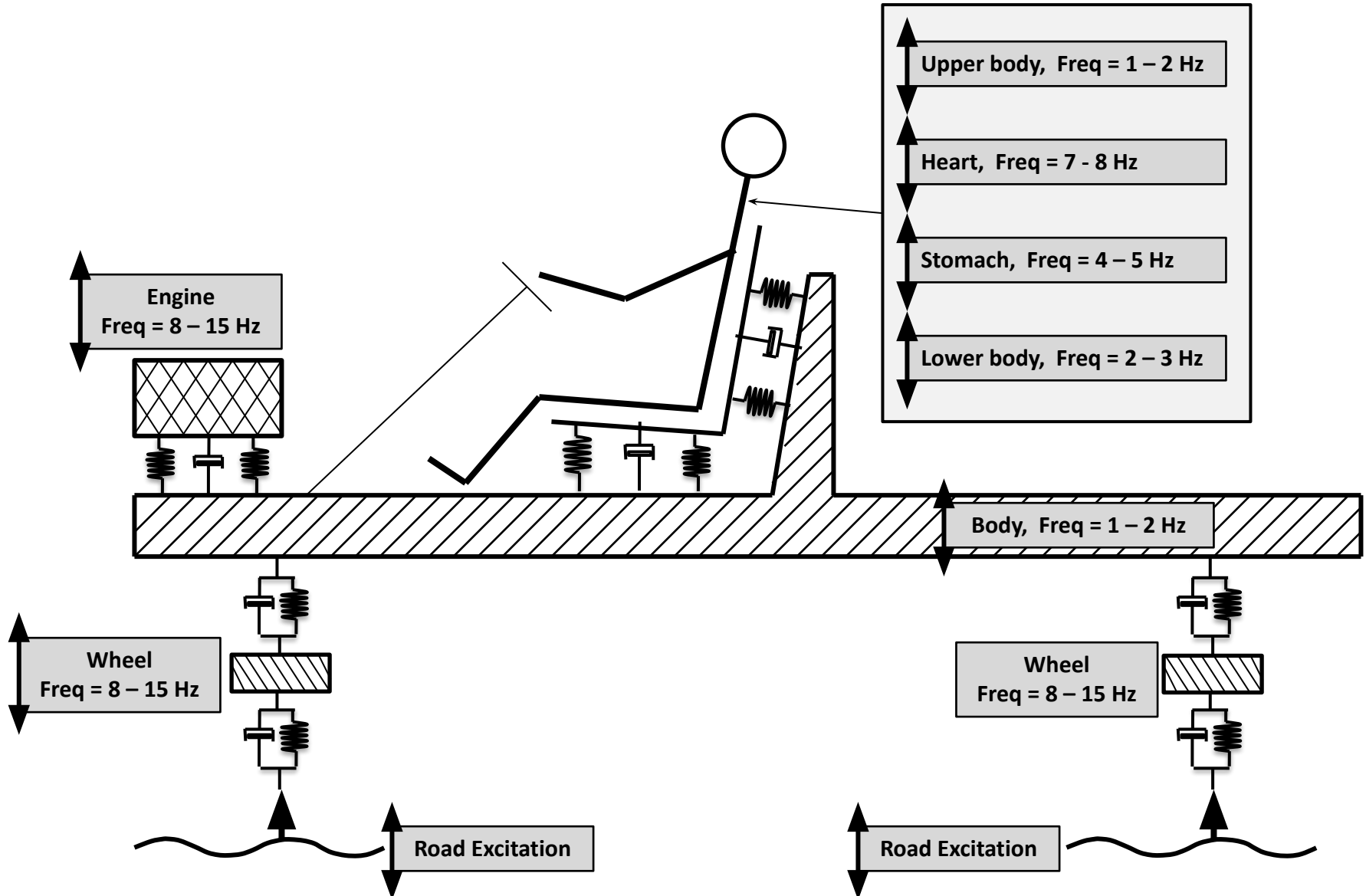


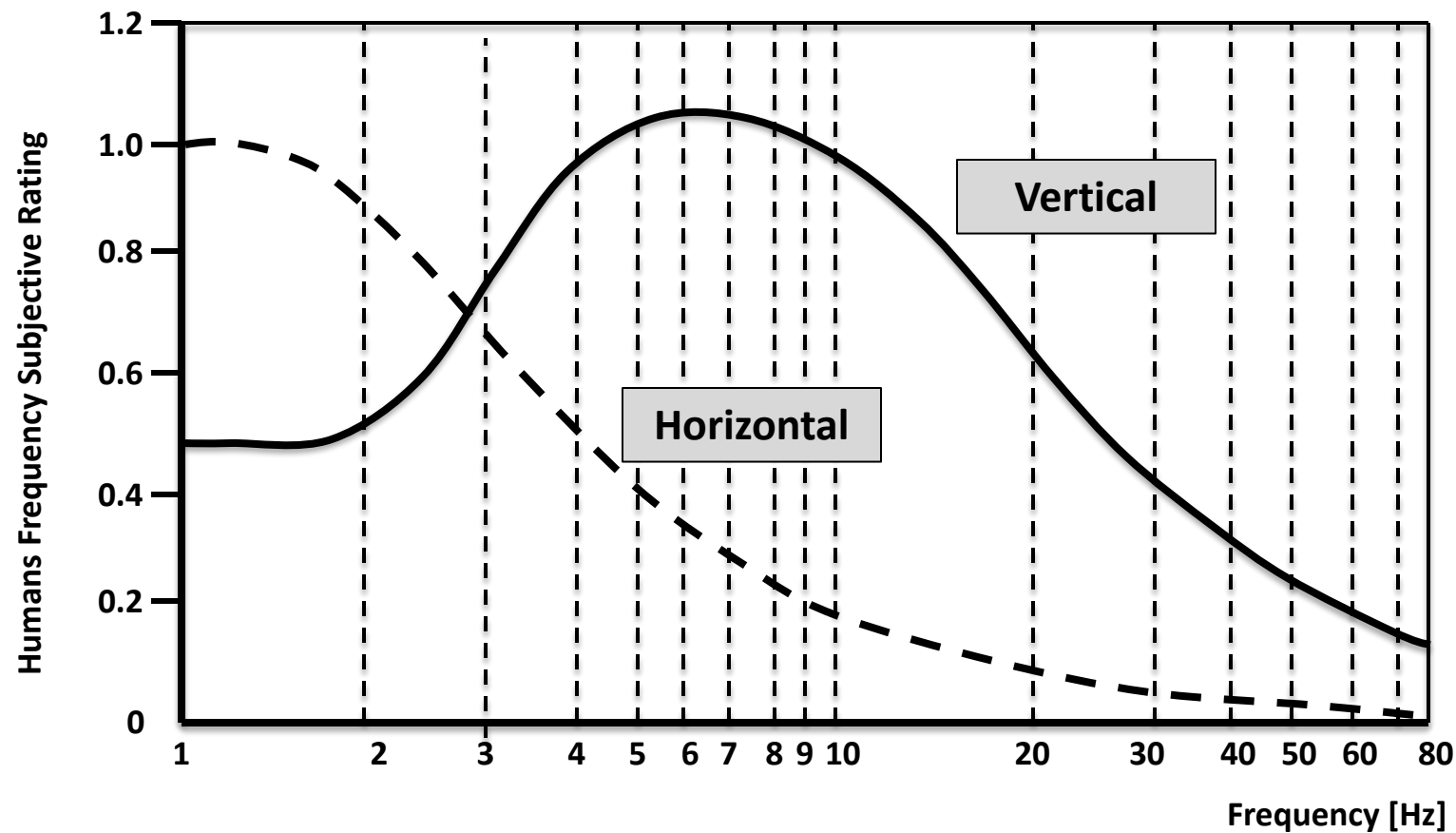


4. Vertical Dynamics

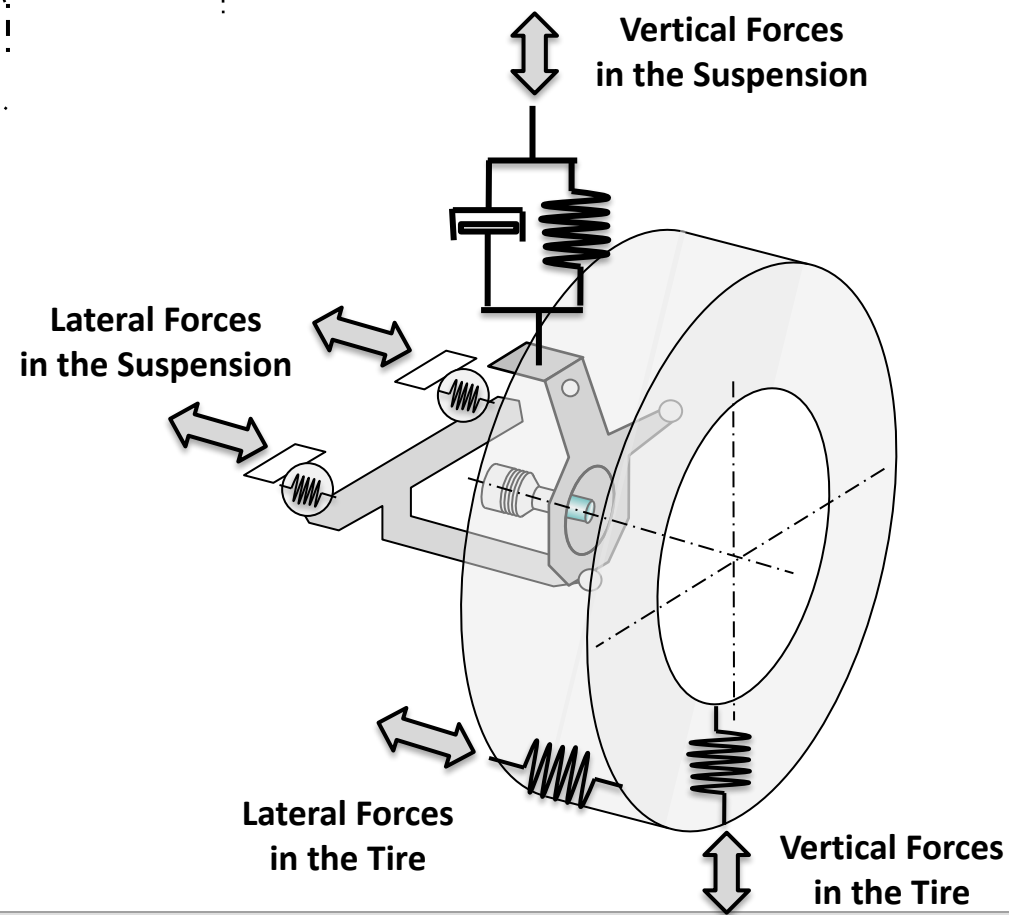
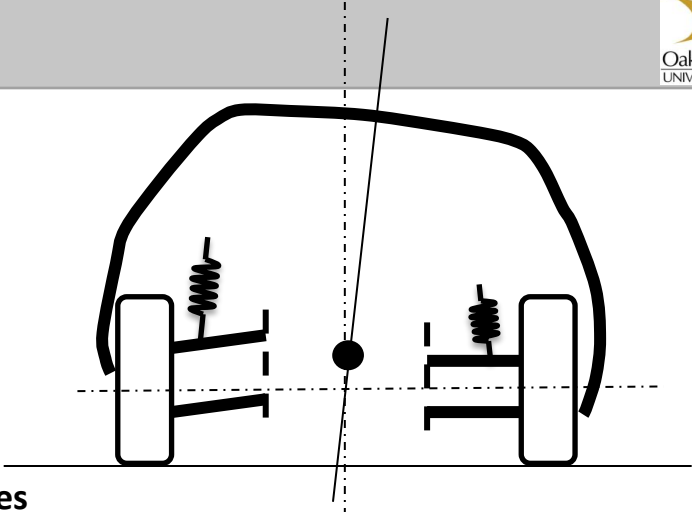
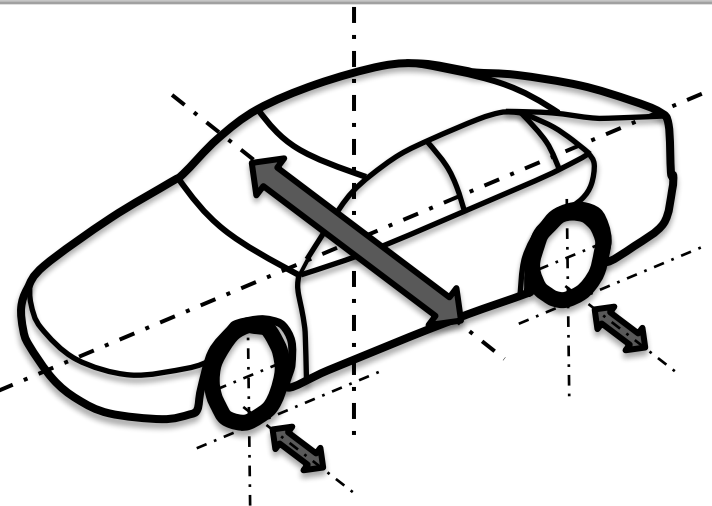
4.3. Road excitation

Vibrations Model: Vehicle / Seat / Human





Frequency Rating Curve for Horizontal and Vertical Vibrations for Humans (seating / standing)

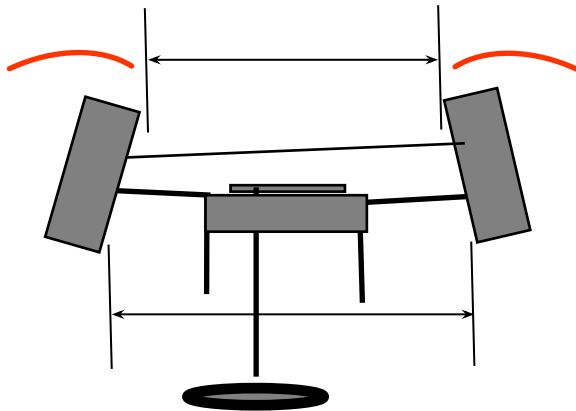


Excitation Forces:

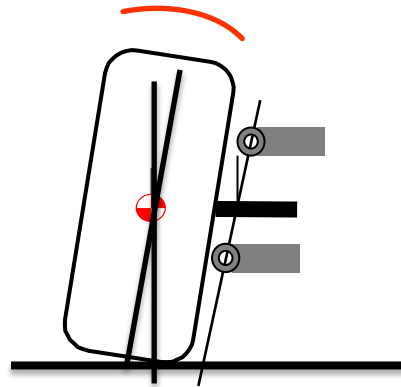
- **Cornering**

Wheel Positions in the suspension

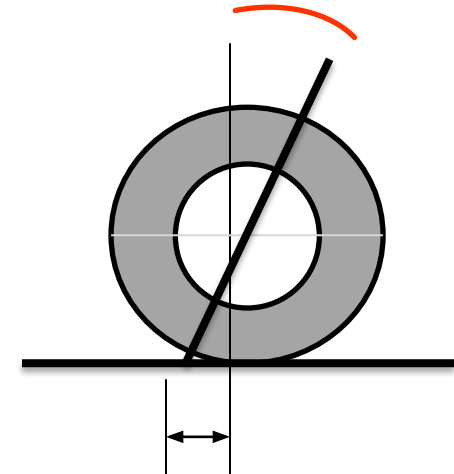
Toe Angle



Camber Angle



Caster Angle

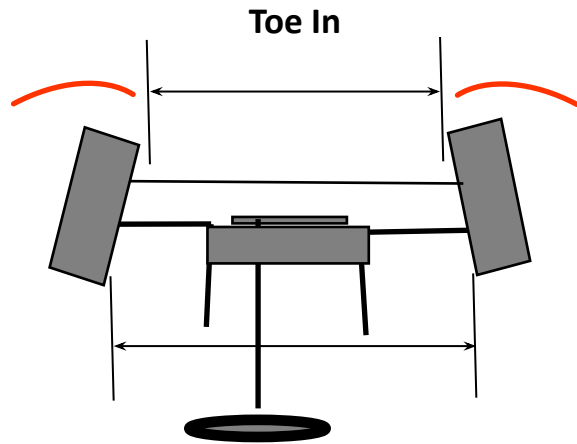


Toe, Camber, Caster

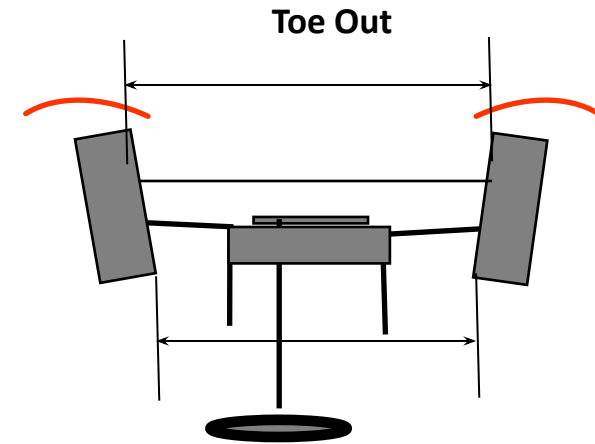
Design and tuning know how was gained at the OEMs from years of extensive testing and simulations, over the decades of suspension development from solid axle to independent wheel suspension.

4. Lateral Dynamics

4.0 Wheel position in the suspension



Toe Angle



Toe Angle Influence:

- Major impact on driving directional stability
- Tire wear / wheel resistance, min wear at 0 degree
- Straight line stability
- Corner entry handling characteristic

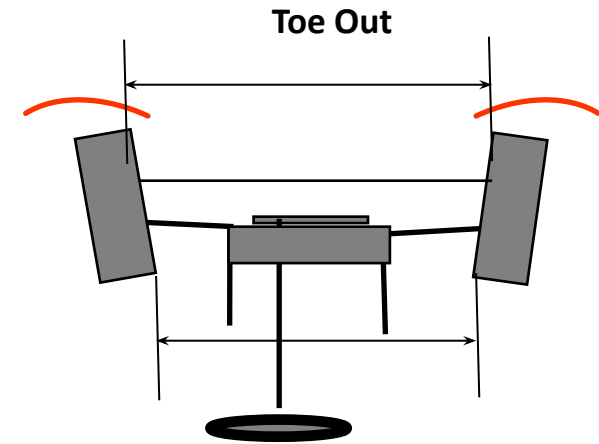
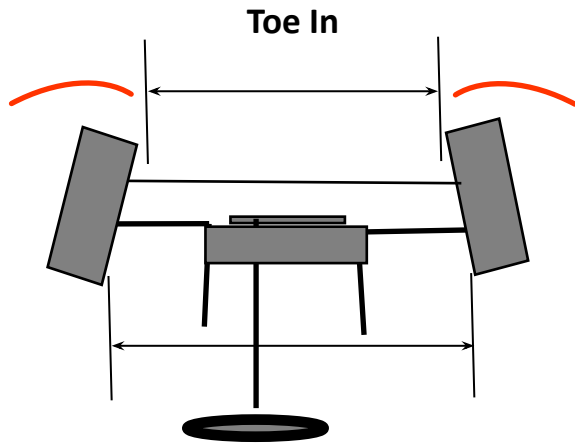
Toe In :

- discourages initiation of turn
- if too extensive, too much tire wear outboard
- enhance straight -line stability
- by small disturbance (due to steering or road / elastokinematic of the suspension) still keeping straight course, not initiating turn

Toe Out :

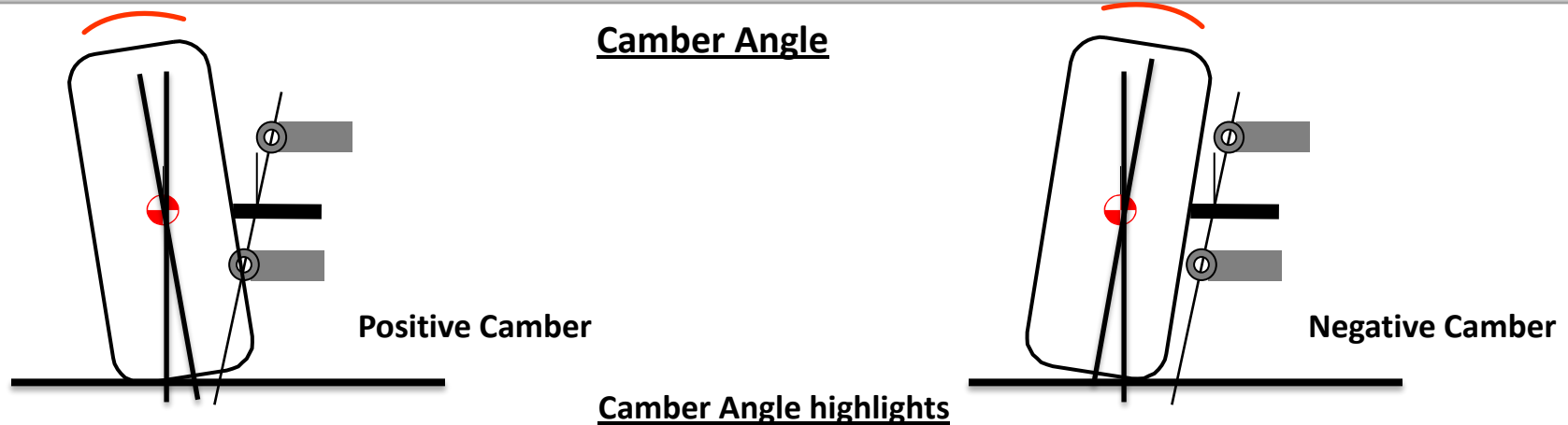
- encourages initiation of turn
- if too extensive, too much tire wear inboard
- by steering, the inboard wheel will try to turn much tighter radius than the outboard wheel

Toe Angle



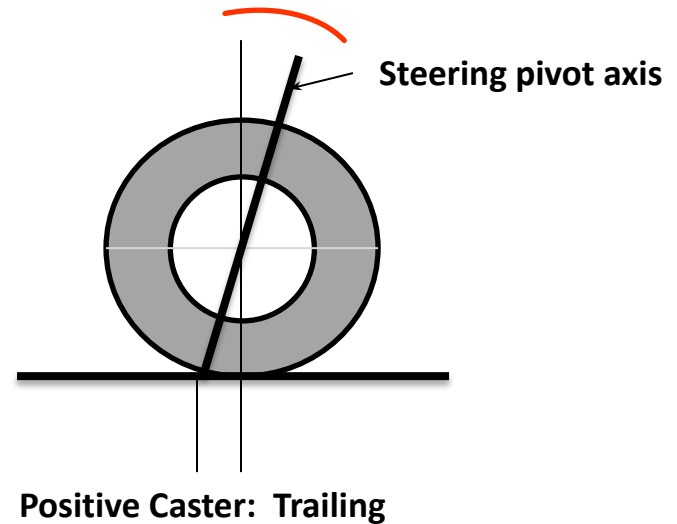
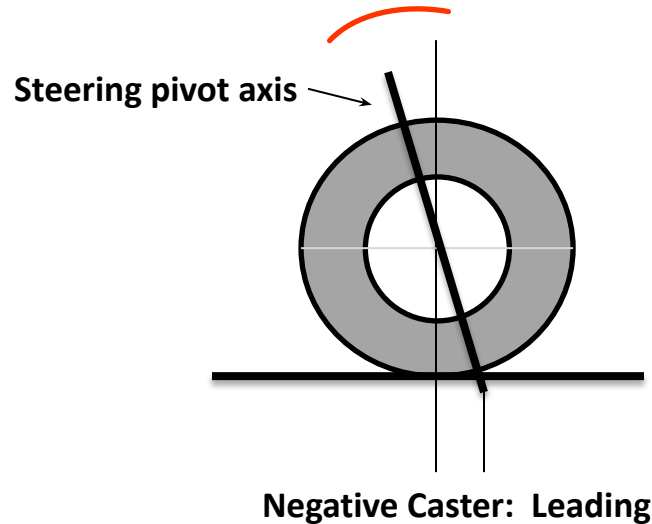
Toe Angle additional points

- Toe settings are a trade off between straight-line stability done by toe-in and quick steering response given by toe-out
- Passenger cars are mostly tuned with toe-in, to ensure good straight line stability.
- Race cars can be tuned with Toe-out to ensure faster and more sensitive turns.
- If rear suspension has independent link suspension design, also toe angle needs to be tuned in order to ensure driving stability and prevent tendency over steering during straight line driving (due to small steering or suspension elastokinematics movements)



- Camber angle is very much influencing tire cornering force
- Major influence on vehicle lateral road holding and stability
- In average tire is developing max cornering force at 0.5 degree negative camber (camber counterbalancing / interacting with the tire deformation: sidewall and tread pattern)
- optimizing vehicle / tire lateral / cornering performance means: developing suspension which is operating always close to ca. 0.5 degree negative camber (this is very difficult because of suspension kinematics and springing and vehicle comfort requirements which are related to soft bushings: elastokinematics)
- during driving / cornering the camber is changing (dynamic camber), camber should:
 - inside wheel gain towards positive camber
 - outside wheel gain towards negative camber
- Dynamic camber definition: very important suspension tuning know how.

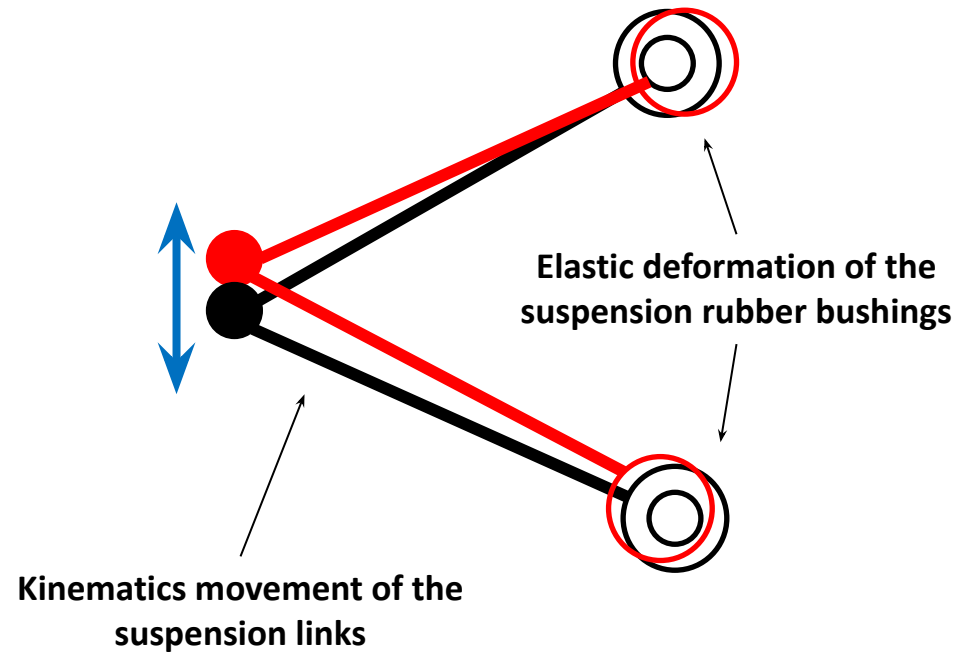
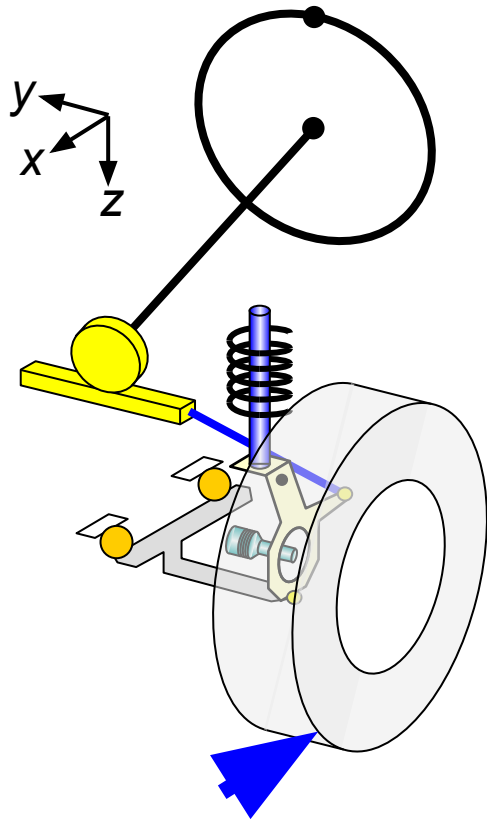
Caster Angle



Positive Caster:

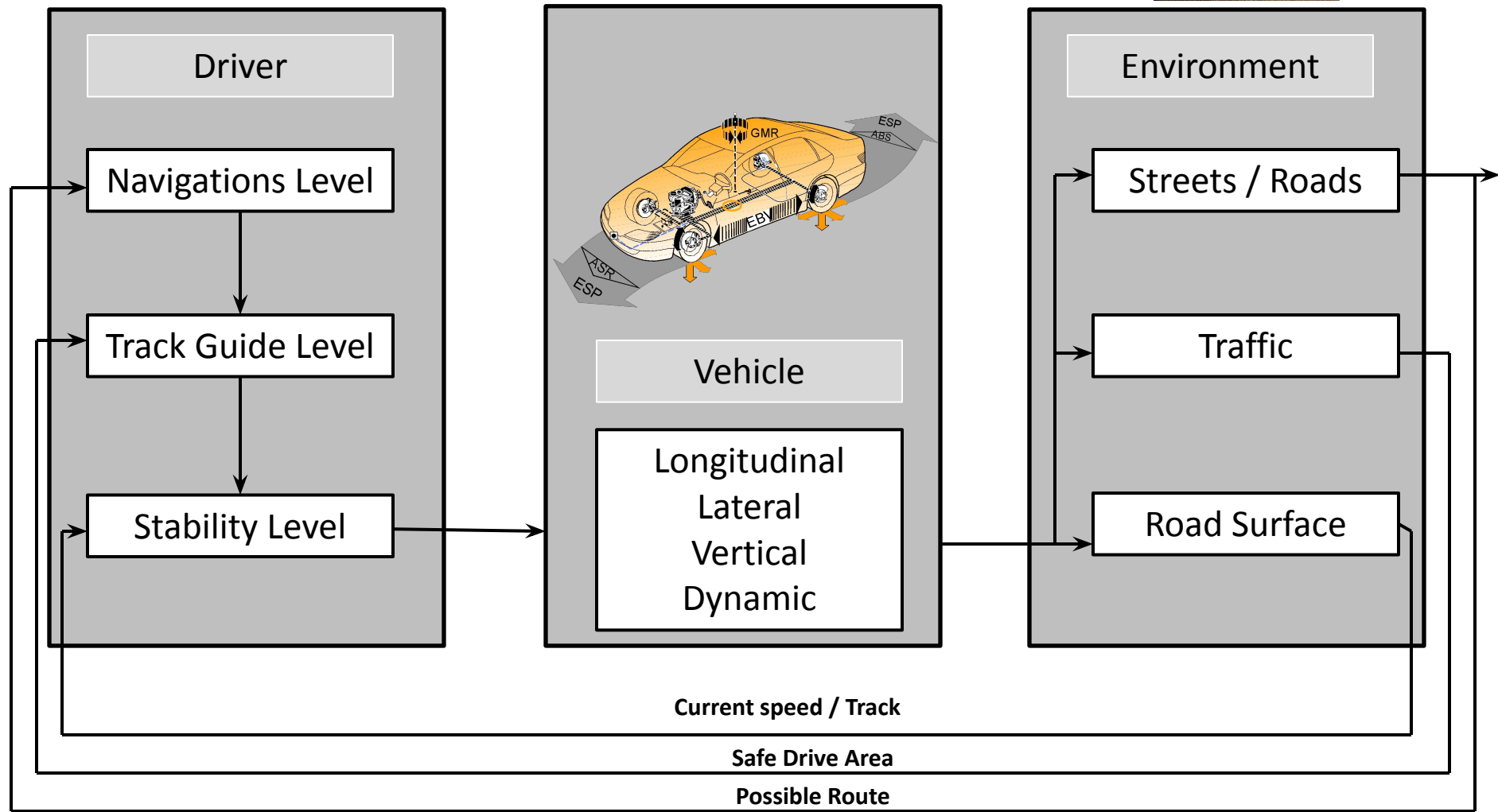
- usually 3 – 5 degree
- utilized in most of the vehicles / front axle
- if front wheels turned: positively influences camber
 - inside wheel is gaining positive camber
 - outside wheel is gaining negative camber
 - both are favorable for cornering

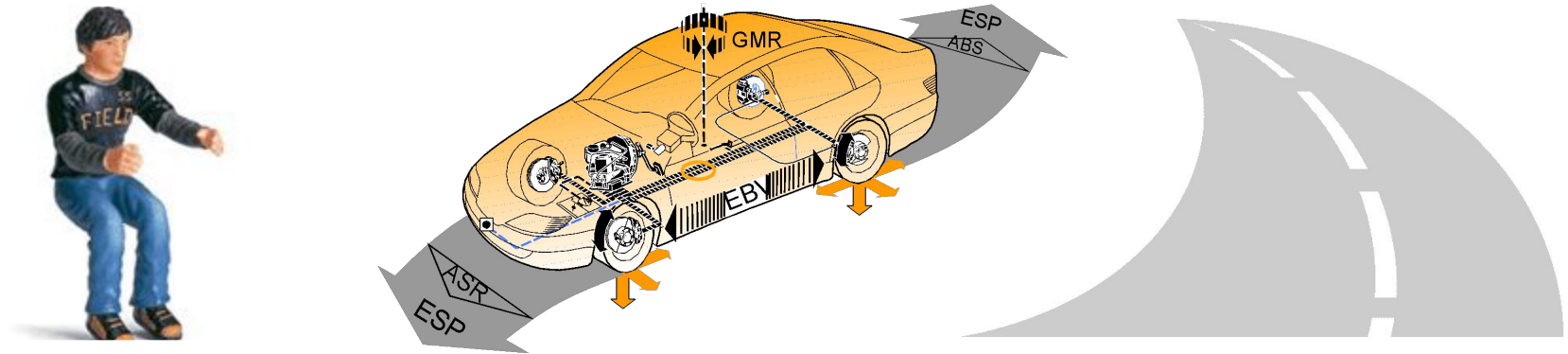
Suspension elastokinematics
of the suspension links and bushings





Driver – Vehicle - Environment
Close Loop Control System:





Control System: Driver – Vehicle – Road/Environment

- Navigation Level
- Track / Course Level
- Stability Level

System Stability depend on:

Driver
Vehicle
Environment

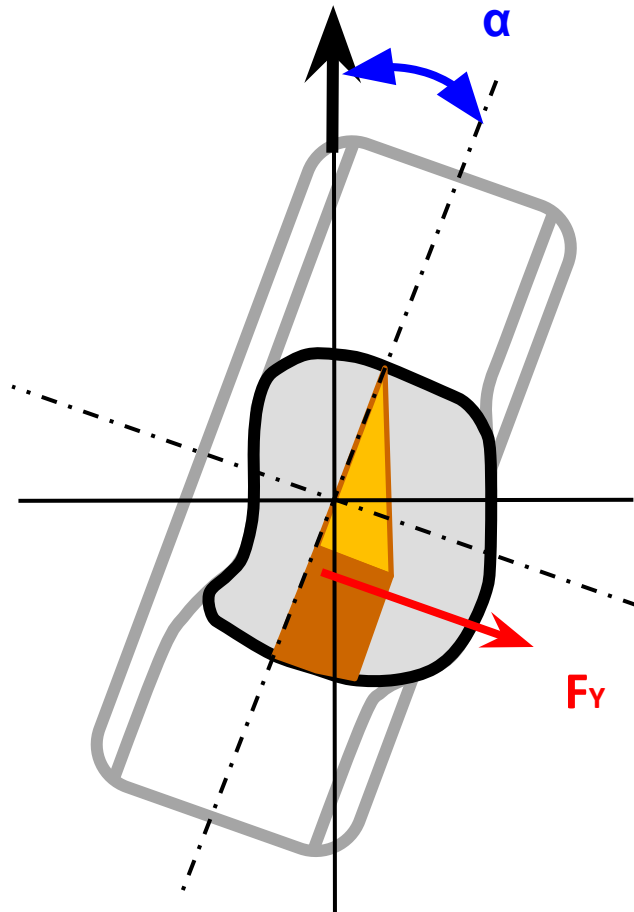
Vehicle Development / Engineering:

□ responsible for the Vehicle System Optimization

- Driver / Vehicle Interaction !!!
- Vehicle / Road Interaction
- Driver / Environment Interaction

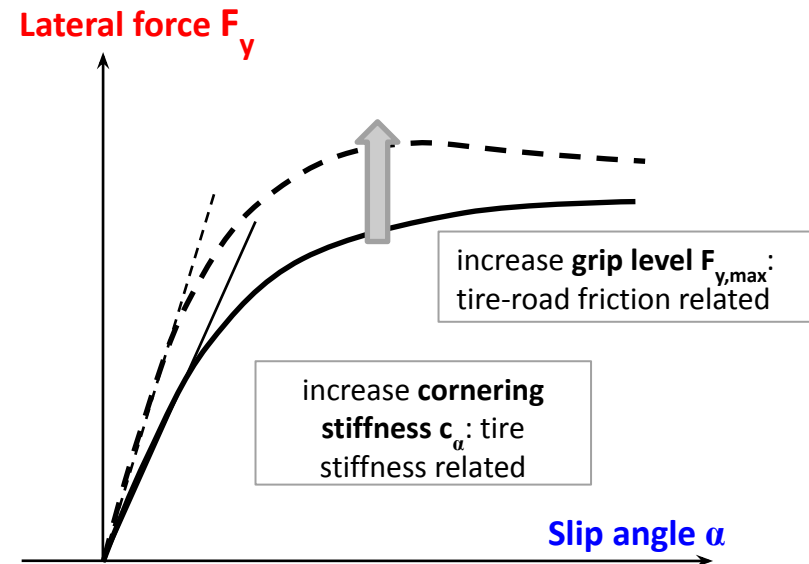
4. Lateral Dynamics

4.1 Lateral acceleration, forces and slip angle



Wheel Slip Angle α , definition:

- Wheel slip angle is the angle between the wheel rolling / heading direction and the direction towards wheel is steering / pointing.
- Slip angle is the result of tire deformation in lateral direction, and it is proportional to the lateral force acting on the tire.
- No lateral force \Rightarrow No lateral deformation \Rightarrow No slip angle

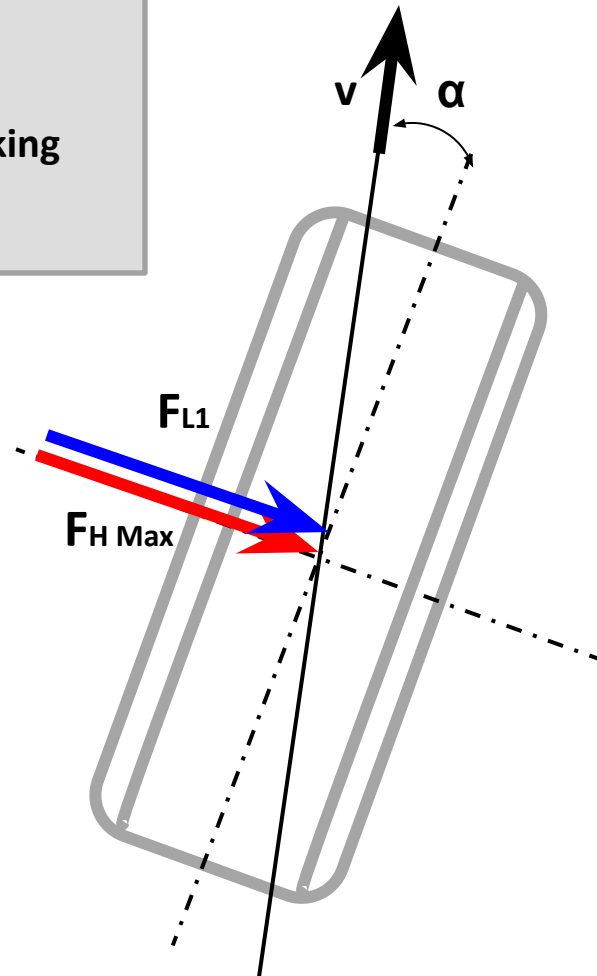


4. Lateral Dynamics

4.1 Lateral acceleration, forces and slip angle

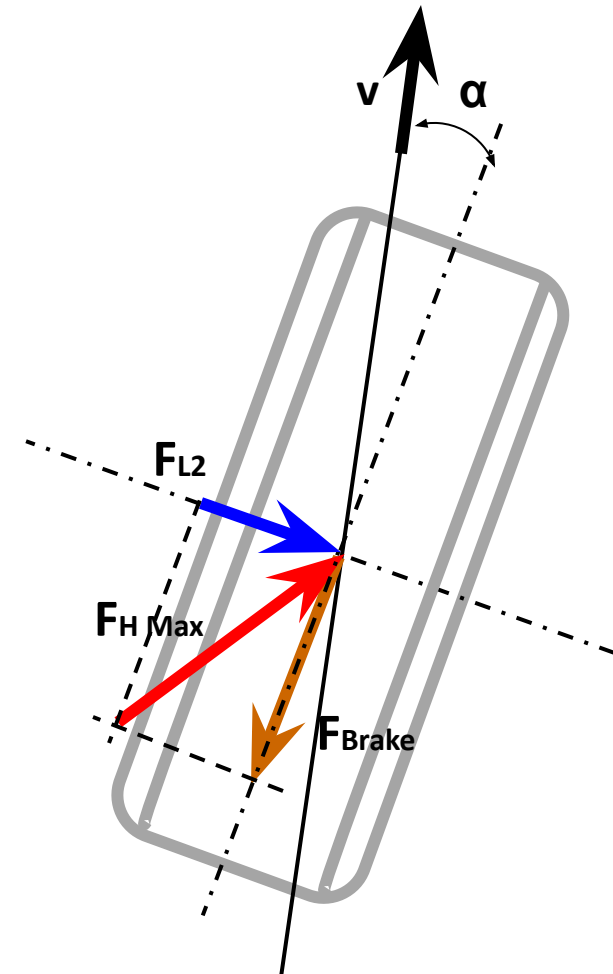
$F_{H \text{ Max}}$	Max Horizontal Force
G_v	Vertical Force
F_{L1}	Lateral Force
F_{L2}	Lateral Force at Braking
F_{Brake}	Brake Force

Cornering ONLY



$$F_{L1} = F_{H \text{ Max}} = G_v \mu$$

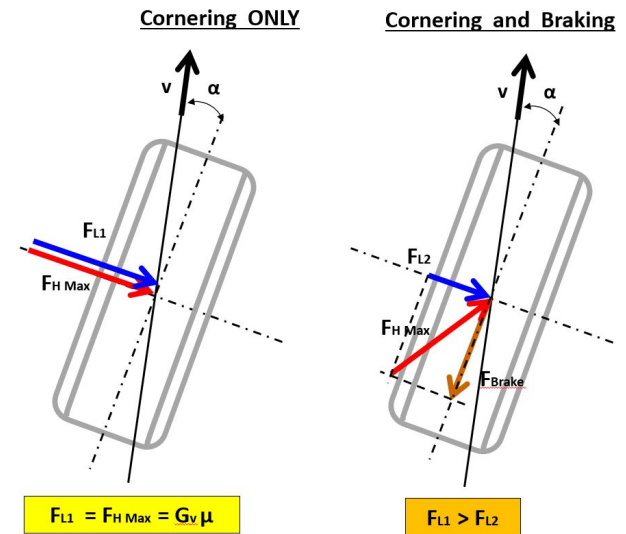
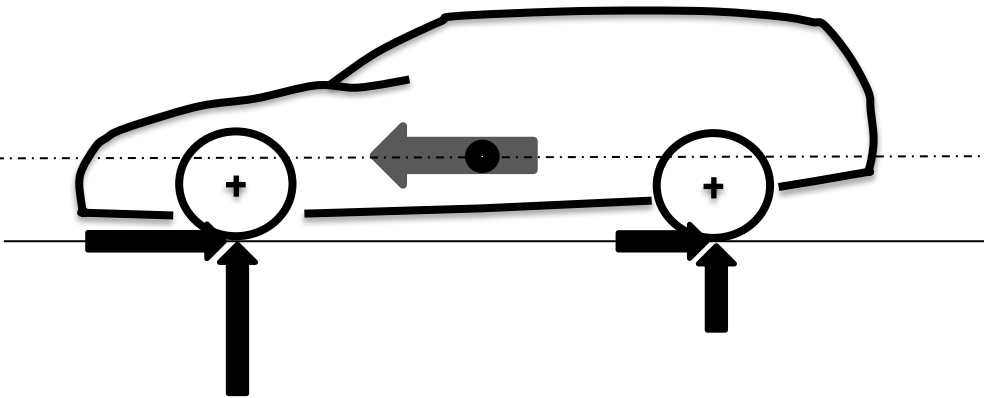
Cornering and Braking



$$F_{L1} > F_{L2}$$

Influence of longitudinal dynamics events on lateral dynamic behavior

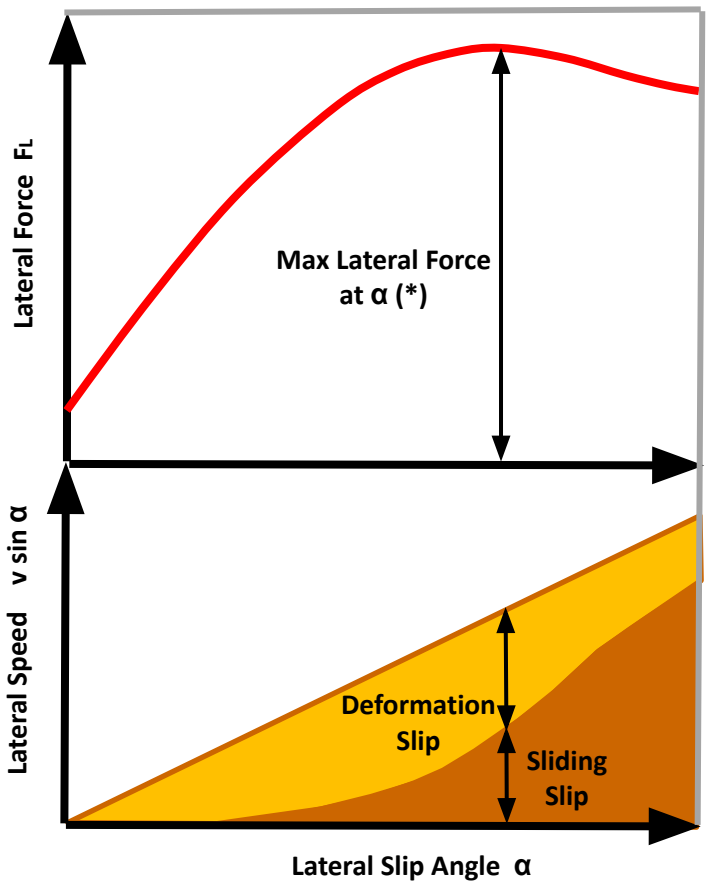
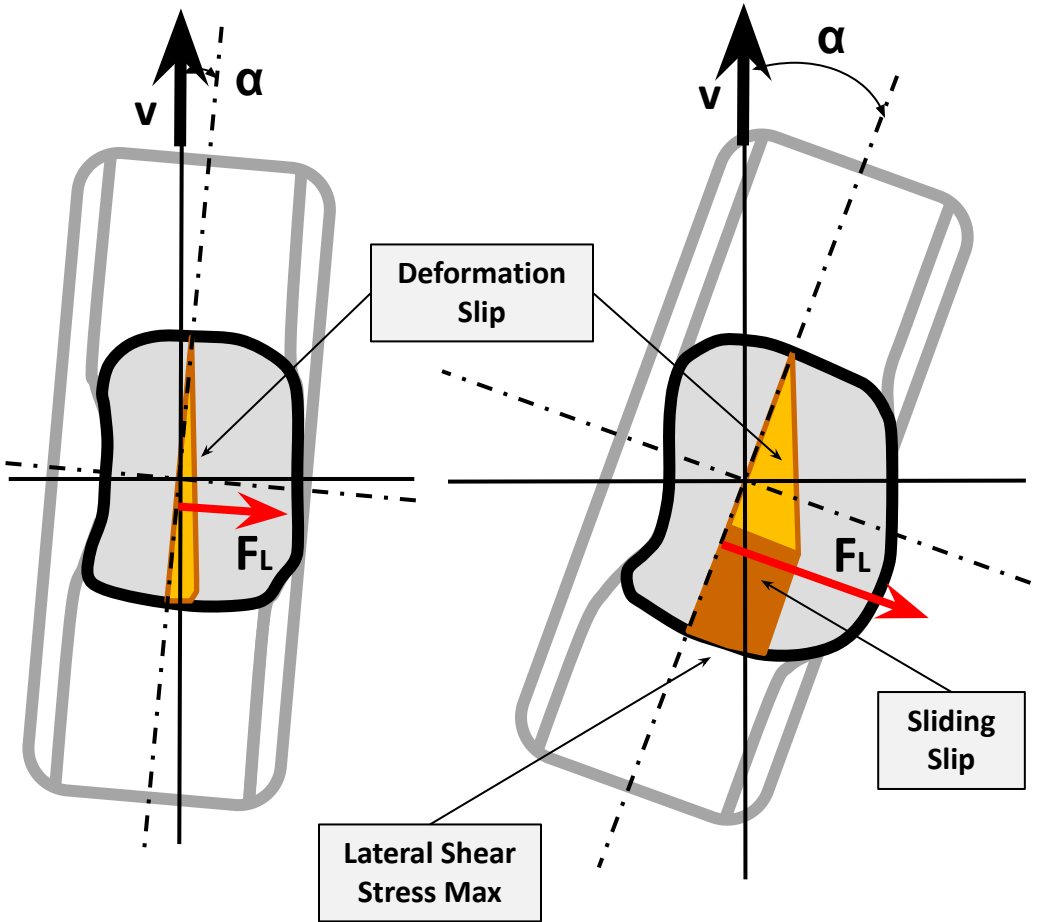
- Acceleration, while cornering
 - Load change, while cornering
 - Braking, while cornering
 - Braking on split μ
- is requiring steering correction compensation



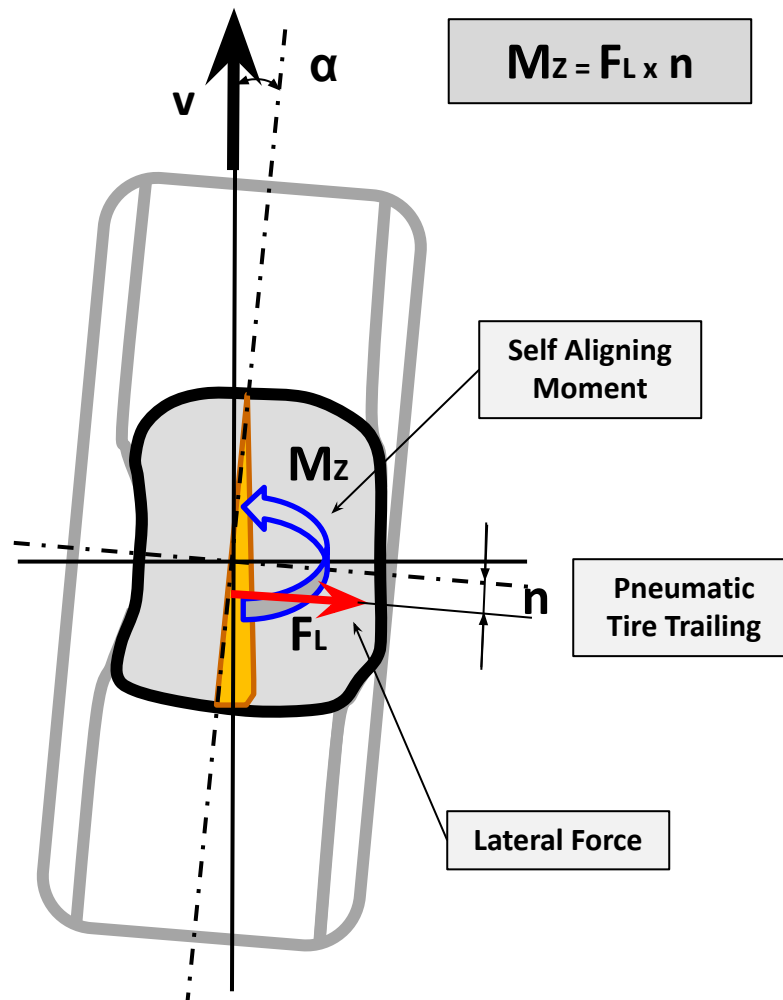
Max available lateral force is changing between front / rear and left / right wheels of the vehicle
Reduction of max available lateral force due to:

- Vertical loads distribution
- Longitudinal force action

Vehicle Cornering, build up of the tire slip in the cornering



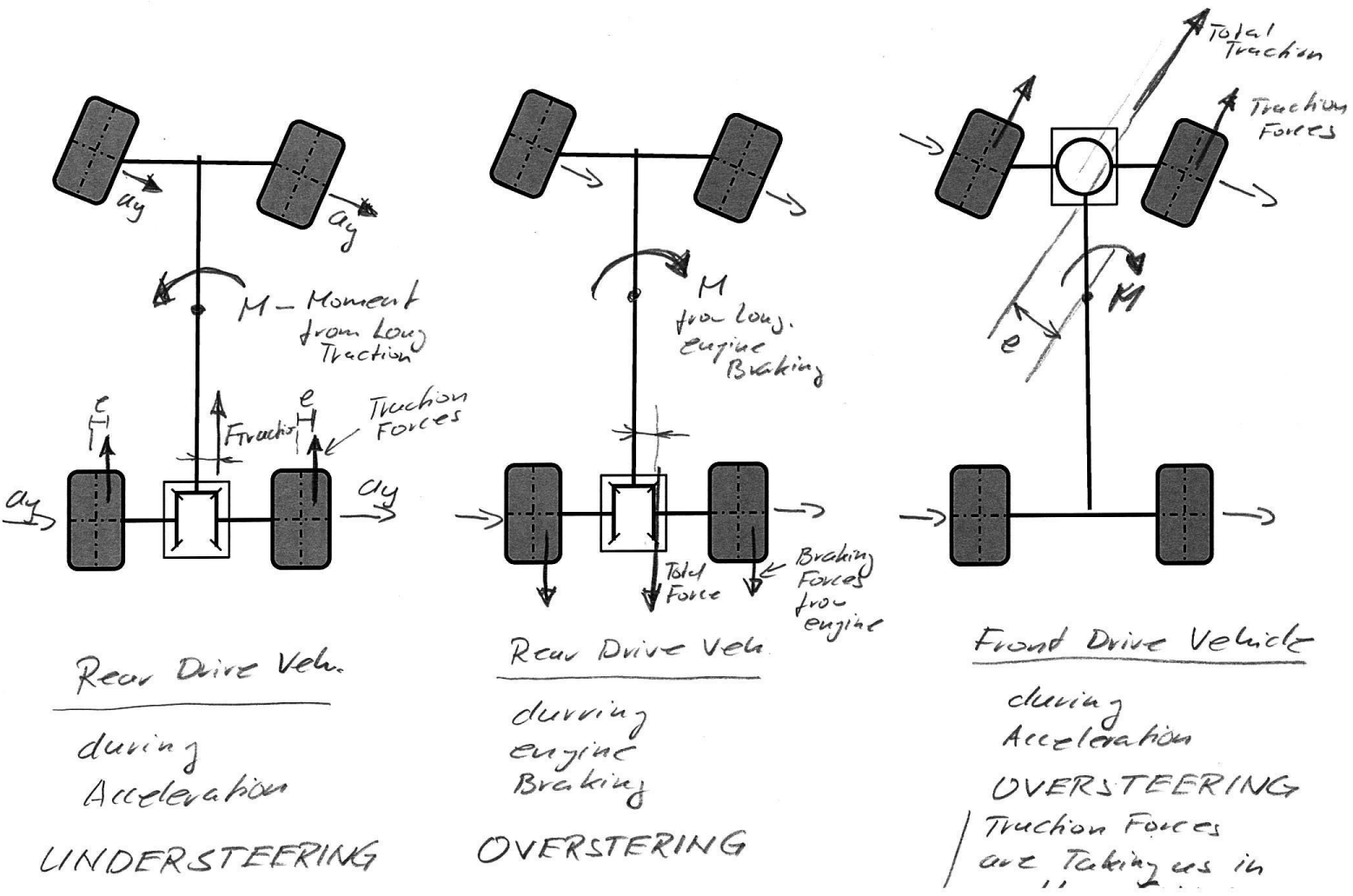
Vehicle Cornering, Self-aligning Moment, Pneumatic Tire Trailing



4. Lateral Dynamics

4.4 Vehicle stationary and non-stationary cornering

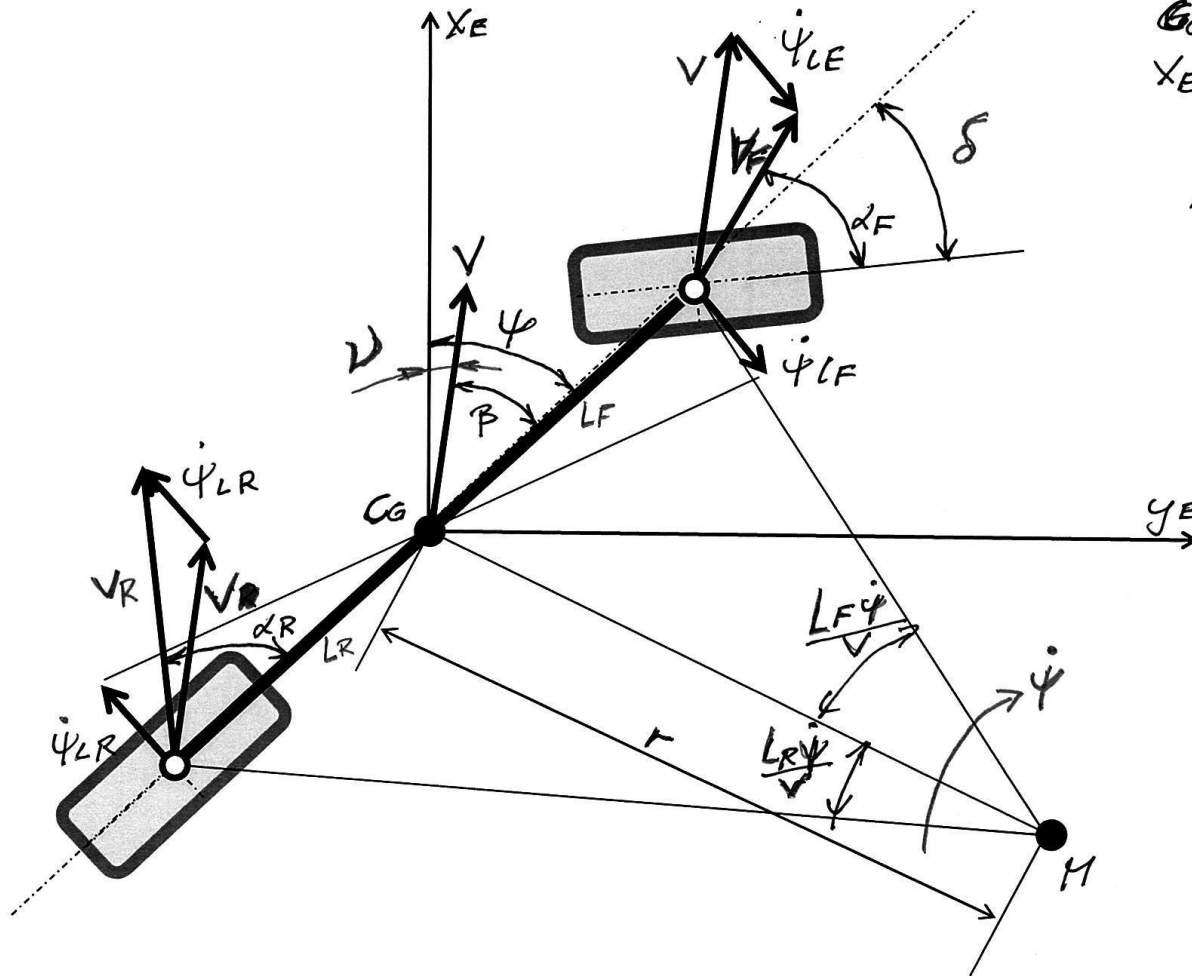
Yaw Moments resulting from the Longitudinal Forces during cornering 230



4. Lateral Dynamics

4.5 Lateral dynamics modeling

Motions Vectors and Parameters of bicycle model



M - Moment of I
 r - course Radius
 G - Centre of Gravity
 X_E, Y_E - stationary coordinate system

Angles

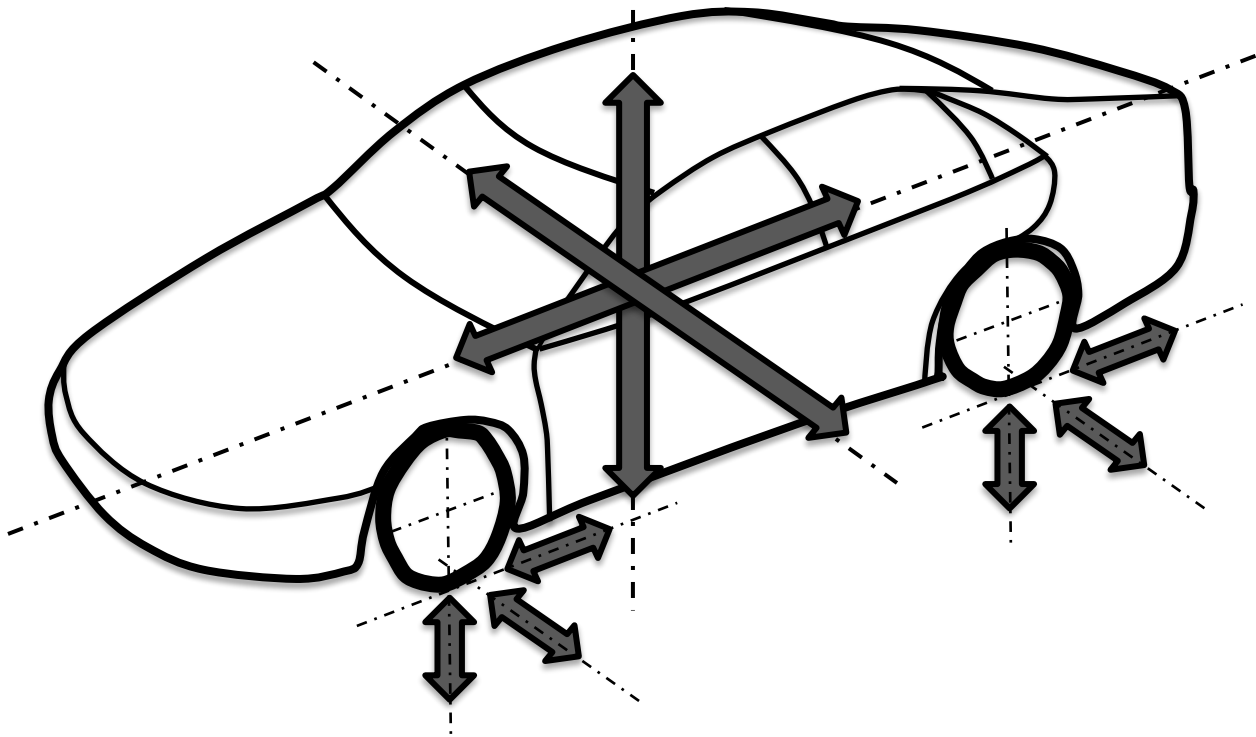
α_F, α_R - Slip Angle Front & Rear
 β - Veh. Slip, drift
 δ - steer Angle
 ψ - yaw Angle
 ψ - course Angle

Speeds

$\dot{\psi}$ - Yaw speed
 $\dot{\psi}_F, \dot{\psi}_R$
 V - speed Veh.
 V_F, V_R - Resulting speed Front and Rear Wheels

5. Interaction between longitudinal, vertical and lateral vehicle motions

5.1. 3-Dimensional Interaction

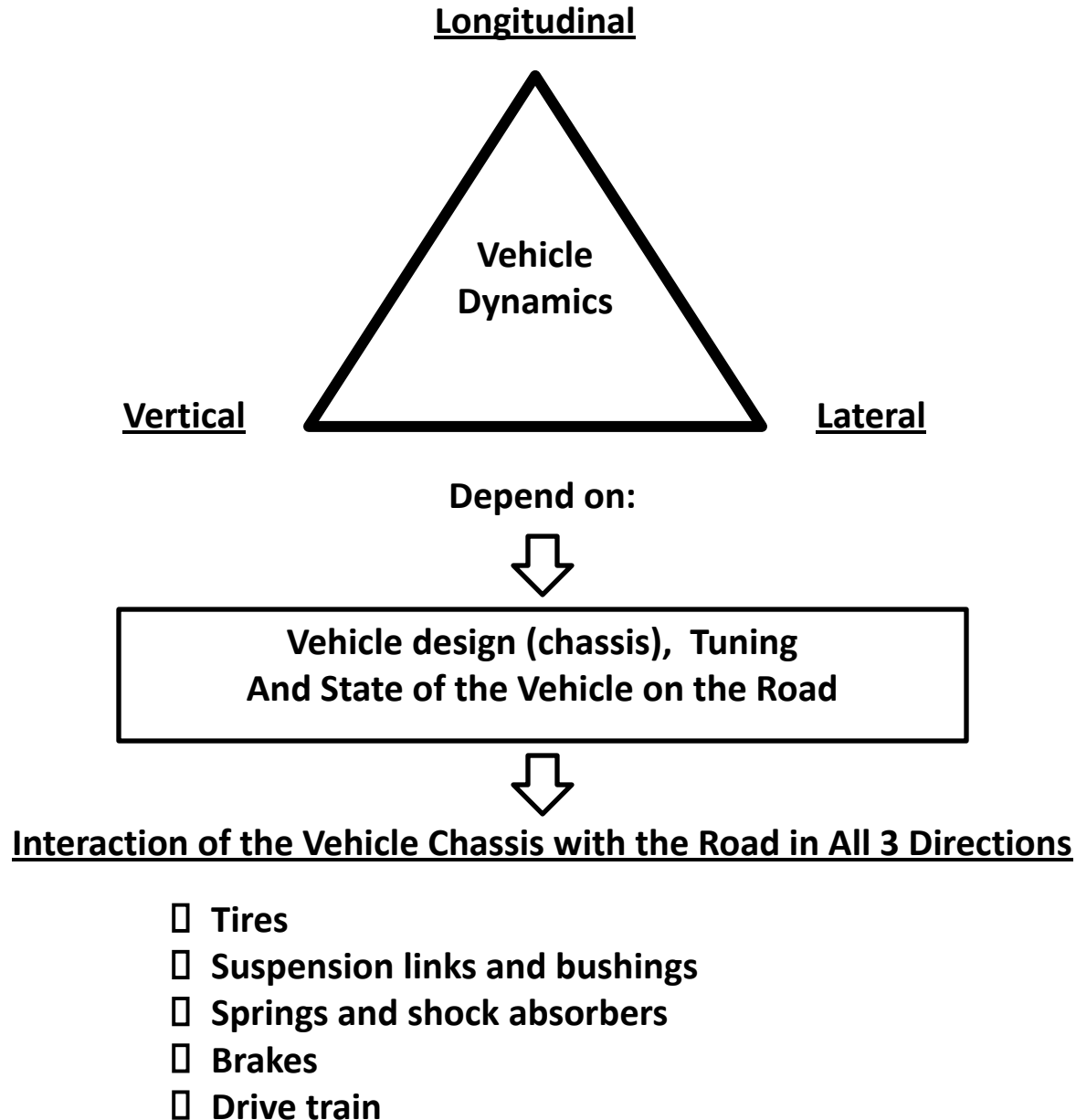


To design and tune vehicle chassis means



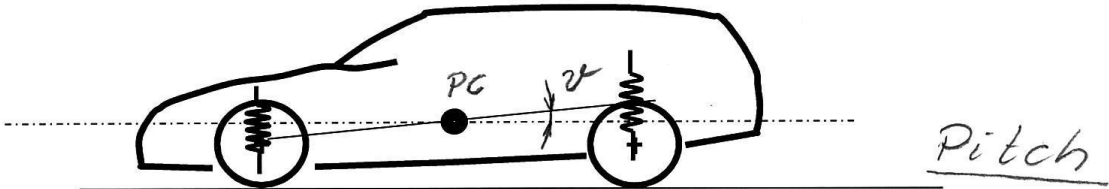
To consider forces / accelerations in all 3 directions at the same time:

- Longitudinal driving forces
- Cornering forces
- Braking forces
- Road interactions forces



5. Interaction between longitudinal, vertical and lateral vehicle motions

5.2 Vehicle Pitch and Roll Motions



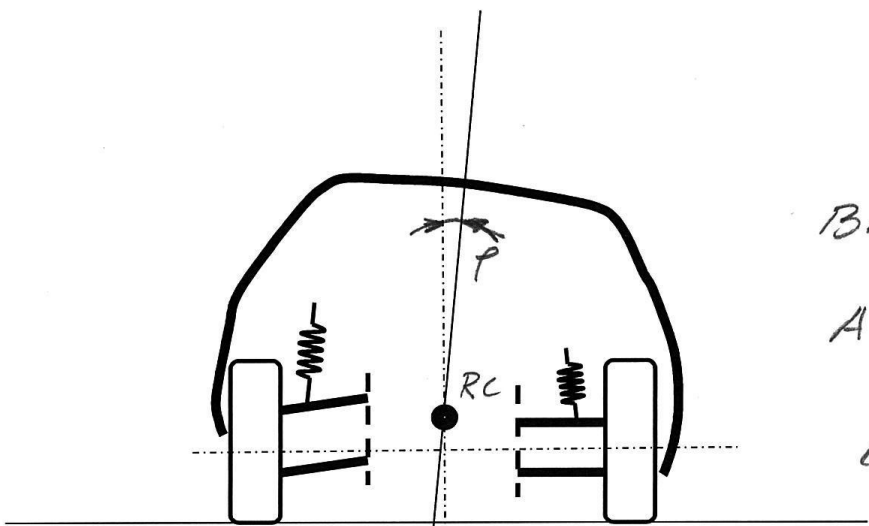
Pitch

(+)

Roll



Braking
or
Accelerating
while
cornering

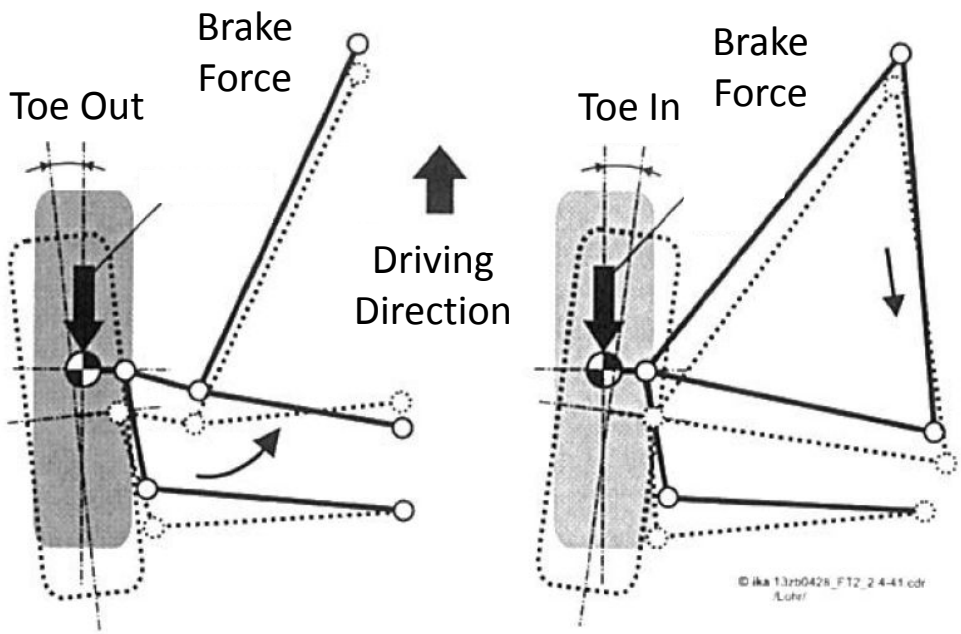
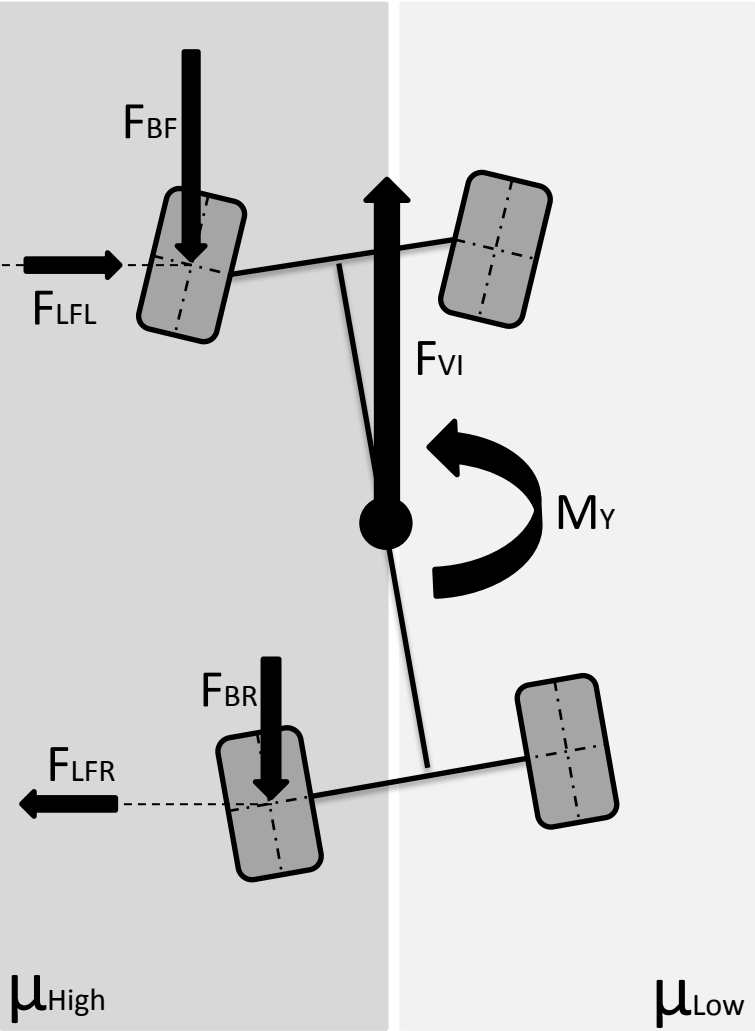


Braking on the Left turn : Front Right Wheel max. Vertical Force (U-Turn in Mi)
Accelerating on the Right turn : Right Rear Wheel max Vertical

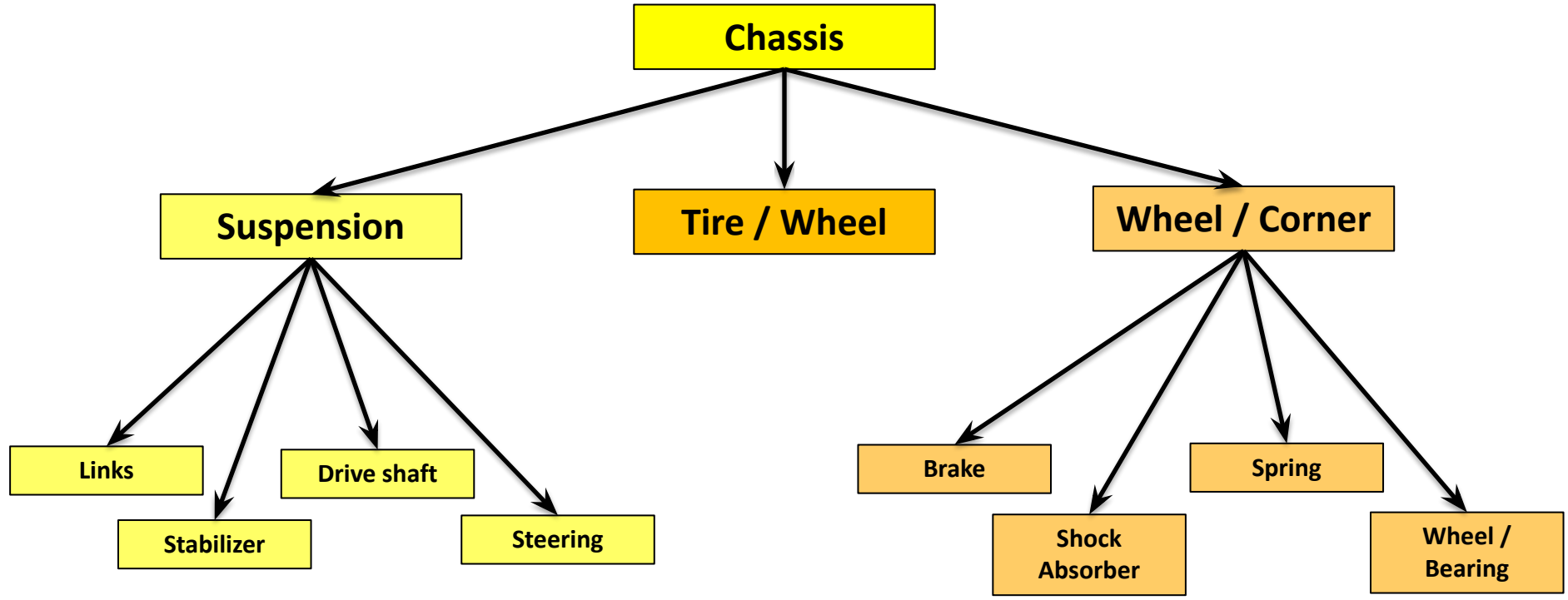
5. Interaction between longitudinal, vertical and lateral vehicle motions

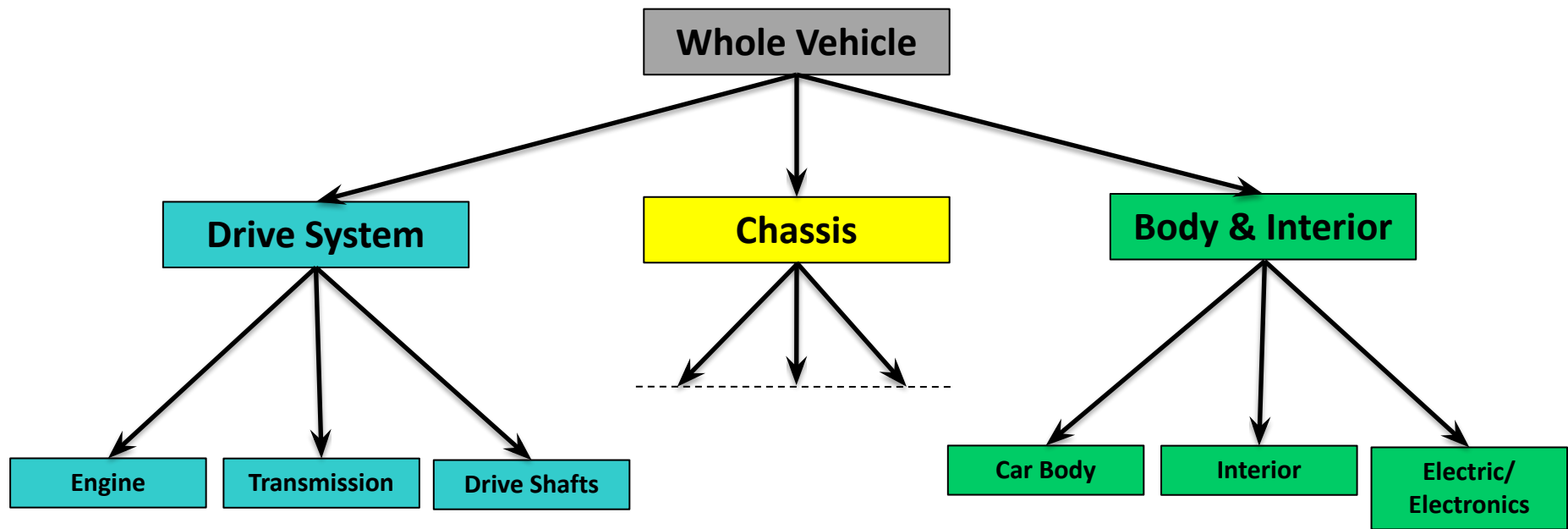
5.6 Braking on split μ surface

Braking on μ -split



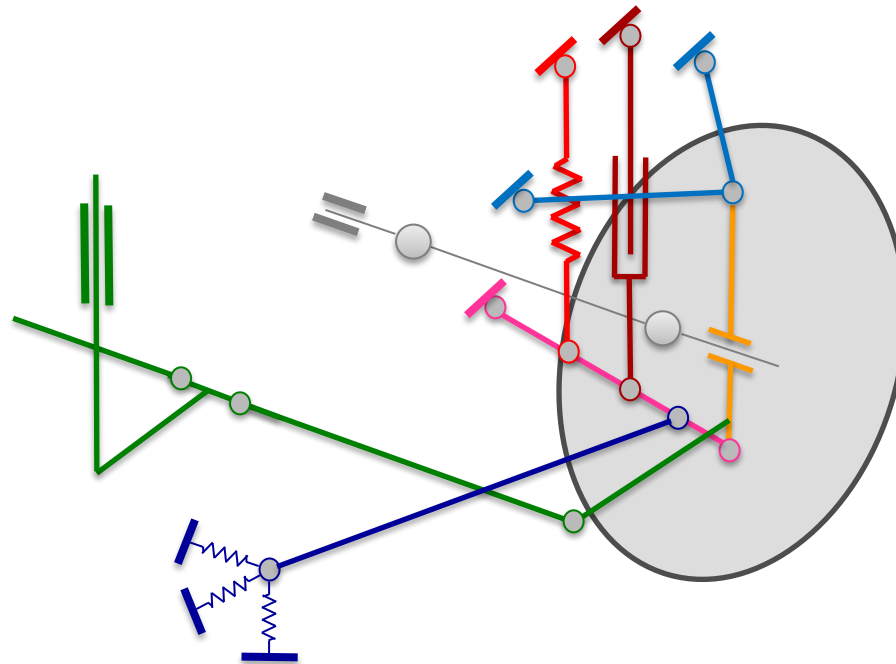
Optimization of
Front Suspension Elasto-Kinematics
for split μ braking



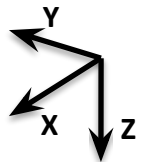


6. Suspension Systems:

6.1 Elements and Function



- Tire/wheel assembly
- Knuckle
- Drive shaft
- Lower lateral links
- Lower longitudinal links
- Upper links
- Spring
- Shock absorber (damper)
- Steering



Tire

Tire is the only one connection point / structure of the vehicle to the road, due to this transmits all forces between the vehicle and the road.

Accordingly it is fundamentally important and most critical to the vehicle driving behavior, especially: longitudinal, vertical and lateral vehicle dynamics

Fundamental Tire Functions:

- Vehicle support on the road, springing, damping: Vertical Dynamics
- Vehicle lateral guide: Lateral Dynamics
- Driving and brake forces transmission: Longitudinal Dynamics

Tire Requirements

The tire required performances and the tire design are strongly connected to each other.

The different tire requirements results in various target conflicts which are always requiring balanced approach in tire design and performance.

1. Safety:

- Maximal adhesion / traction at all roads surfaces, especially: wet, snow, ice.
- Direct handling response in the steering wheel.
- Evenly distributed lateral / cornering force (rise/increase), good lateral force guide in connection with intended handling maneuvers, good handling predictability.
- Balancing the wheel vertical force variations (to big: negatively influencing the road structure, to small: negatively influencing safety)
- Secure connection / seat on the rim
- High puncture safety
- High speed reliability
- Long life

Tire Requirements

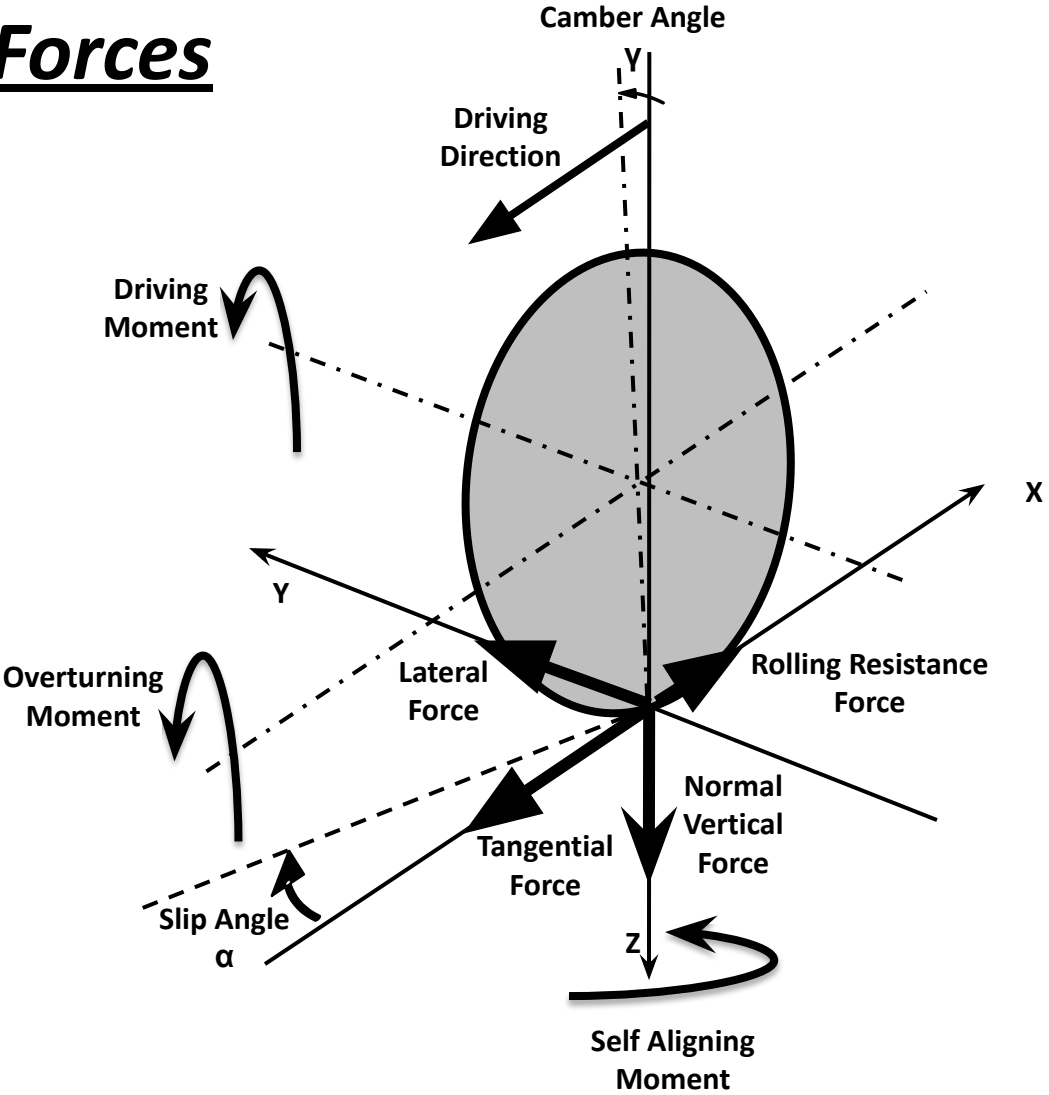
2. Comfort

- ☐ Good springing and damping
- ☐ Low noise: interior, exterior, pass by
- ☐ No vibrations or noises from tire nonuniformity
- ☐ Small as possible steering forces
- ☐ Simple replacement

3. Sustainability / Economics

- ☐ Low as possible rolling resistance
- ☐ High performance capacity at small volume
- ☐ Low as possible road dynamic forces
- ☐ Costs optimized
- ☐ Good durability
- ☐ Constant / even wear
- ☐ Long lasting

Tire Forces



Tire Forces

Comment

- *Braking forces (moment) are supported by brake and suspension*
- *Driving forces (moment) are supported by differential, with it in the wheel mid point*

Tangential Forces :

- Traction forces
- Braking forces
- Rolling resistance



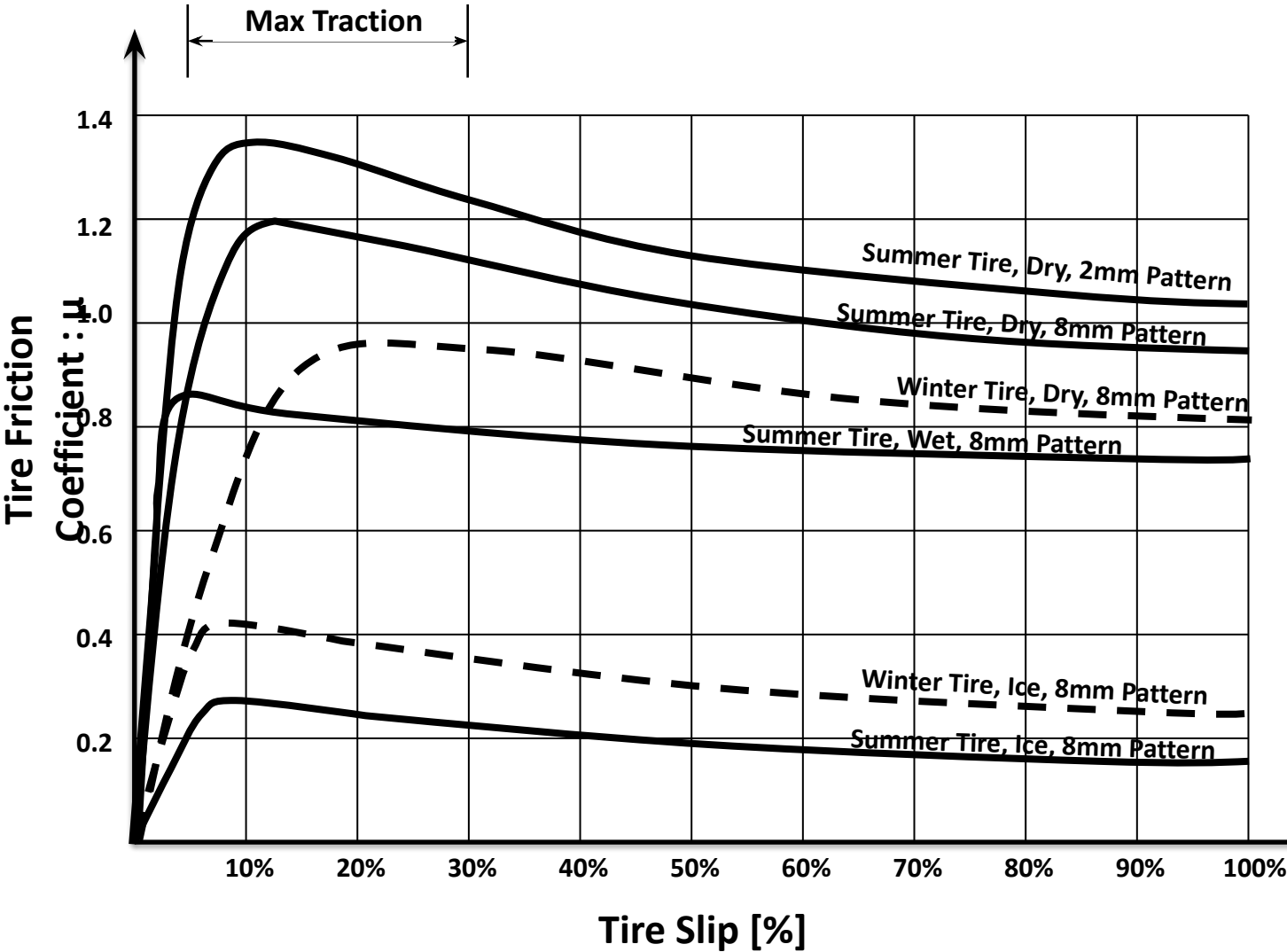
Vertical:

- Wheel load, road interaction (static, dynamic)
- Vibration forces caused by Road roughness (comfort, coustic)

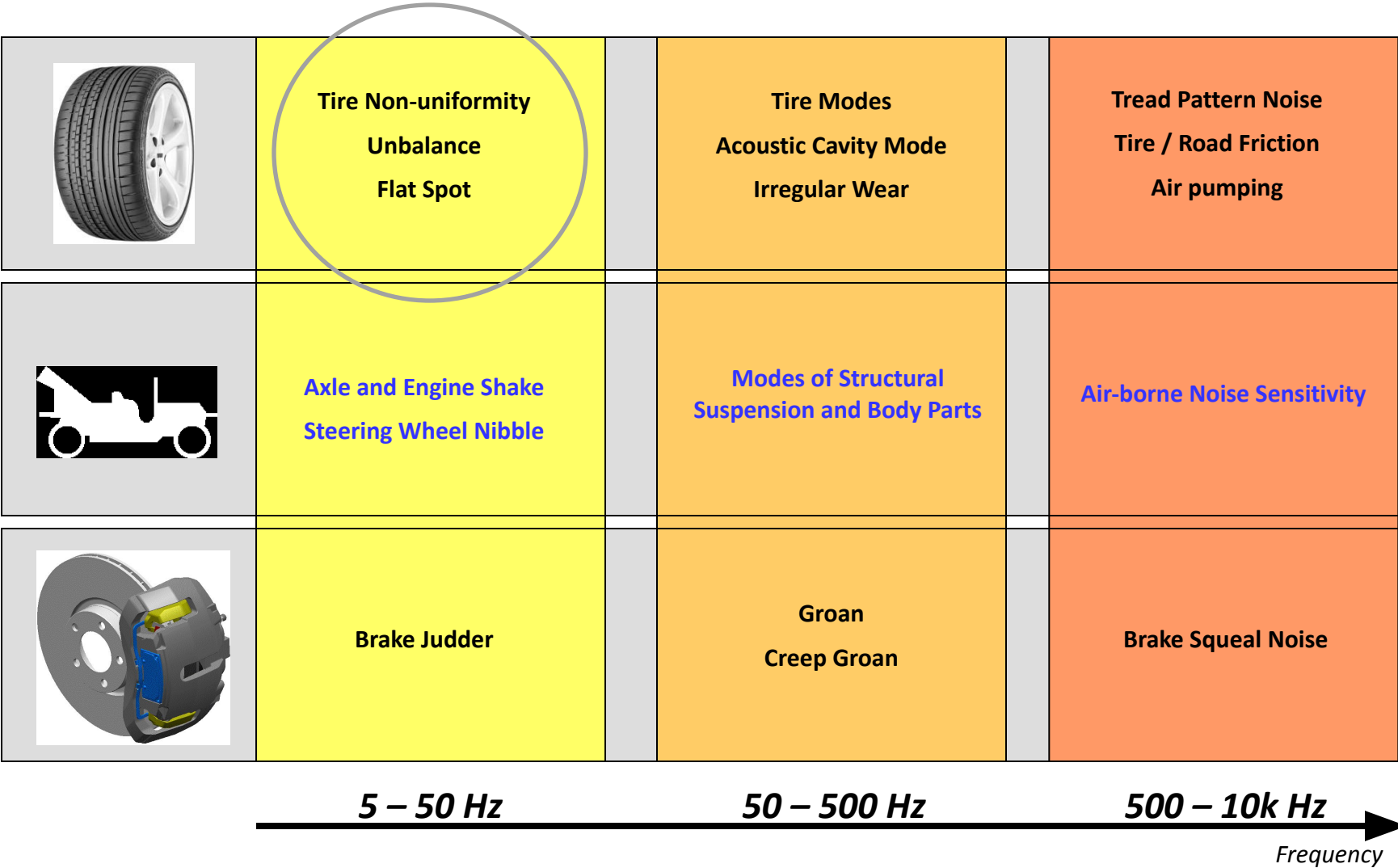
Lateral / Side Forces:

- Lateral forces
- Steering forces
- Aligning moment (self-aligning torque)

Influence of the road surface on tire tangential slip



Tire Nonuniformity as one of the vehicle periodic wheel excitations



Chassis vibration system due to tire periodic excitation

